

Excitons in atomically thin transition metal dichalcogenides

Gang Wang, Alexey Chernikov, Mikhail Glazov, Tony F. Heinz, Xavier Marie, Thierry Amand, Bernhard Urbaszek

To cite this version:

Gang Wang, Alexey Chernikov, Mikhail Glazov, Tony F. Heinz, Xavier Marie, et al.. Excitons in atomically thin transition metal dichalcogenides. Reviews of Modern Physics, 2018, 90 (2), 10.1103/RevModPhys.90.021001. hal-02057678

HAL Id: hal-02057678 <https://insa-toulouse.hal.science/hal-02057678v1>

Submitted on 14 May 2019

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

CHORUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

Colloquium: Excitons in atomically thin transition metal dichalcogenides

Gang Wang, Alexey Chernikov, Mikhail M. Glazov, Tony F. Heinz, Xavier Marie, Thierry Amand, and Bernhard Urbaszek

Rev. Mod. Phys. **90**, 021001 — Published 4 April 2018

DOI: [10.1103/RevModPhys.90.021001](http://dx.doi.org/10.1103/RevModPhys.90.021001)

Excitons in atomically thin transition metal dichalcogenides

Gang Wang

Université de Toulouse, INSA-CNRS-UPS, LPCNO, 135 Av. Rangueil, 31077 Toulouse, France *

Alexey Chernikov

Department of Physics, University of Regensburg, D-93040 Regensburg, Germany

Mikhail M. Glazov

Ioffe Institute, 194021 St. Petersburg, Russia

Tony F. Heinz

Department of Applied Physics, Stanford University, Stanford, California 94305, USA and SLAC National Accelerator Laboratory, 2575 Sand Hill Road, Menlo Park, California 94025, USA

Xavier Marie, Thierry Amand and Bernhard Urbaszek

Université de Toulouse, INSA-CNRS-UPS, LPCNO, 135 Av. Rangueil, 31077 Toulouse, France

Atomically thin materials such as graphene and monolayer transition metal dichalcogenides (TMDs) exhibit remarkable physical properties resulting from their reduced dimensionality and crystal symmetry. The family of semiconducting transition metal dichalcogenides is an especially promising platform for fundamental studies of two-dimensional (2D) systems, with potential applications in optoelectronics and valleytronics due to their direct band gap in the monolayer limit and highly efficient light-matter coupling. A crystal lattice with broken inversion symmetry combined with strong spin-orbit interactions leads to a unique combination of the spin and valley degrees of freedom. In addition, the 2D character of the monolayers and weak dielectric screening from the environment yield a significant enhancement of the Coulomb interaction. The resulting formation of bound electron-hole pairs, or excitons, dominates the optical and spin properties of the material. Here we review recent progress in our understanding of the excitonic properties in monolayer TMDs and lay out future challenges. We focus on the consequences of the strong direct and exchange Coulomb interaction, discuss exciton-light interaction and effects of other carriers and excitons on electron-hole pairs in TMDs. Finally, the impact on valley polarization is described and the tuning of the energies and polarization observed in applied electric and magnetic fields is summarized.

Contents

[Acknowledgments](#page-23-1) 22

[References](#page-24-0) 23

I. INTRODUCTION

Atomically thin transition metal dichalcogenides (TMDs) have unique physical properties which could be of value for a broad range of applications [\(Butler](#page-24-1) et al., [2013;](#page-24-1) [Castellanos-Gomez,](#page-24-2) [2016;](#page-24-2) [Geim and Grigorieva,](#page-25-0) [2013;](#page-25-0) [Mak and Shan,](#page-26-0) [2016;](#page-26-0) [Wang](#page-28-0) et al., [2012b;](#page-28-0) Xia [et al.](#page-28-1), [2014;](#page-28-1) Xu [et al.](#page-28-2), [2014;](#page-28-2) Yu [et al.](#page-29-0), [2015a\)](#page-29-0). The investigation of bulk and thin layers of TMDs can be traced back decades [\(Bromley](#page-24-3) et al., [1972;](#page-24-3) [Frindt,](#page-25-1) [1966;](#page-25-1) [Wil](#page-28-3)[son and Yoffe,](#page-28-3) [1969\)](#page-28-3), but starting with the emergence of graphene [\(Novoselov](#page-26-1) et al., [2004,](#page-26-1) [2005\)](#page-26-2), many additional techniques for producing, characterizing, and manipulating atomically thin flakes were developed. This led to rapid progress in the study of monolayers of other van der Waals systems like the TMDs. Monolayer (ML) $MoS₂$ is a typical member of the group VI TMD family of the form MX_2 and was isolated in early studies, for

example in [Frindt](#page-25-1) [\(1966\)](#page-25-1); [Joensen](#page-25-2) et al. [\(1986\)](#page-25-2); here M is the transition metal (Mo, W) and X the chalcogen (S, Se, Te), see Fig. [1a](#page-5-1). However, only around 2010, were the TMDs confirmed to be direct band gap semiconductors in monolayer form, with up to 20% absorption per monolayer at the exciton resonance depending on the spectral region (Mak [et al.](#page-26-3), [2010;](#page-26-3) [Splendiani](#page-27-0) et al., [2010\)](#page-27-0). These discoveries launched intense research activity exploring the electronic properties and physics of single- and fewlayer TMDs.

The transition metal chalcogenides are a group of about 60 materials, most of which are layered structures in their bulk form with weak interlayer van-der-Waals interactions [\(Wilson and Yoffe,](#page-28-3) [1969\)](#page-28-3). By using micromechanical cleavage (commonly referred to as exfoliation or "scotch-tape technique"), one can obtain few-layer and monolayer crystals, typically a few to tens of micrometers in lateral dimension [\(Castellanos-Gomez](#page-24-4) et al., [2014\)](#page-24-4). There are currently vigorous efforts to grow large-area TMD monolayes by chemical vapor deposition (CVD) [\(Zhan](#page-29-1) et al., [2012\)](#page-29-1) and by van der Waals epitaxy in ultrahigh vacuum [\(Xenogiannopoulou](#page-28-4) et al., [2015;](#page-28-4) [Zhang](#page-29-2) [et al.](#page-29-2), [2014b\)](#page-29-2), but many of the intriguing properties reviewed here were identified in high-quality monolayers prepared from naturally occurring or synthesized bulk crystals by exfoliation.

In this review we mainly concentrate on group VI semiconducting dichalcogenides with M=Mo, W and X=S, Se, Te which share fascinating excitonic properties and provide unique opportunities to optically manipulate spin and valley states. These monolayers are stable enough under ambient conditions to perform optical and electrical characterization. With respect to the electronic structure, they are indirect band gap semiconductors in their bulk form [\(Bromley](#page-24-3) et al., [1972\)](#page-24-3). When thinned down to the limit of a single monolayer, the band gap becomes direct. The corresponding band extrema are located at the finite momentum K^+ and K^- points of the hexagonal Brillouin zone and give rise to interband transitions in the visible to near-infrared spectral range. In the literature, the energy states close to the $K^+/K^$ points located at the edges of the first Brillouin zone are typically referred to as K^+ and K^- valleys, whereas the term valley is generally used to designate band extrema in momentum space. The presence of a direct gap is particularly interesting for potential device applications because of the associated possibility for efficient light emission. Promising device prototypes have already been demonstrated with diverse functionality, including phototransitors based on monolayer $MoS₂$ [\(Lopez-Sanchez](#page-26-4) *et al.*, [2013\)](#page-26-4), sensors [\(Perkins](#page-26-5) et al., [2013\)](#page-26-5), logic circuits [\(Radis](#page-27-1)[avljevic](#page-27-1) et al., [2011b;](#page-27-1) [Wang](#page-28-5) et al., [2012a\)](#page-28-5), and light producing and harvesting devices [\(Cheng](#page-24-5) et al., [2014;](#page-24-5) [Lopez-](#page-26-6)[Sanchez](#page-26-6) et al., [2014;](#page-26-6) [Pospischil](#page-27-2) et al., [2014;](#page-27-2) Ross [et al.](#page-27-3), [2014\)](#page-27-3) among others. In addition to being direct, the optical transitions at the gap are also valley selective, as σ^+ and σ^- circularly polarized light can induce optical transitions only at the K^+ and K^- valleys, respectively [\(Cao](#page-24-6)

[et al.](#page-24-6), [2012;](#page-24-6) Xiao [et al.](#page-28-6), [2012\)](#page-28-6). This is in strong contrast to systems such as GaAs and many other III-V and II-VI semiconductors, where the bandgap is located at the center of the Brillouin zone (Γ-point). In comparison to graphene, an additional interesting feature of these materials is the presence of strong spin-orbit interactions, which introduce spin splitting of several hundred meV in the valence band and of a few to tens of meV in the conduction bands [\(Kosmider](#page-26-7) et al., [2013;](#page-26-7) Molina-Sánchez [et al.](#page-26-8), [2013;](#page-26-8) Xiao [et al.](#page-28-6), [2012\)](#page-28-6), where the spin states in the inequivalent valleys K^+ and K^- are linked by time reversal symmetry.

Since their emergence in 2010, the properties of these direct-gap monolayer materials with valley selective optical selections rules have been investigated in detail using both linear and nonlinear optical spectroscopic techniques. In a semiconductor, following absorption of a photon with suitable energy, an electron is promoted to the conduction band, leaving behind a hole in the valence band. In TMD MLs the electrons and holes are tightly bound together as excitons by the attractive Coulomb interaction, with typical binding energies on the order of 0.5 eV [\(Cheiwchanchamnangij and Lambrecht,](#page-24-7) [2012;](#page-24-7) [Chernikov](#page-24-8) et al., [2014;](#page-24-8) He [et al.](#page-25-3), [2014;](#page-25-3) Qiu [et al.](#page-27-4), [2013;](#page-27-4) [Ramasubramaniam,](#page-27-5) [2012;](#page-27-5) [Wang](#page-28-7) et al., [2015a\)](#page-28-7). As a result, the fundamental optical properties at both cryogenic and room temperatures are determined by strong exciton resonances. At the corresponding transition energies, the light-matter interaction is strongly enhanced in comparison to the transitions in the continuum of unbound electrons and holes. While the exciton radii are small, their properties remain to a large extent within the Wannier-Mott regime and preserve analogies to the electronic structure of the hydrogen atom. For these materials with almost ideal 2D confinement and reduced dielectric screening from the environment, the Coulomb attraction between the hole and the electrons is one to two orders of magnitude stronger than in more traditional quasi-2D systems such as GaAs or GaN quantum wells used in today's optoelectronic devices [\(Chichibu](#page-24-9) et al., [1996\)](#page-24-9). Nevertheless, despite important differences, the optical properties of ML TMDs show similarities to the exciton physics studied in detail in GaAs or ZnSe quantum wells [\(Bradford](#page-24-10) et al., [2001;](#page-24-10) [Maialle](#page-26-9) et al., [1993;](#page-26-9) [Pelekanos](#page-26-10) et al., [1992;](#page-26-10) [Vinattieri](#page-28-8) et al., [1994\)](#page-28-8), for example, rendering these systems a useful benchmark for comparing certain optical properties. Moreover, the Coulomb interaction in TMD MLs also determines the valley polarization dynamics of excitons and contributes to the splitting between optically bright and dark exciton states, in addition to spin-orbit coupling. Overall, the physics of these robust excitons are both of fundamental interest and of crucial importance for engineering and exploiting the properties of these materials in potential applications. These factors motivate this short review, which aims to present the current state of the art, as well as open questions that need to be addressed.

The basics of the band structure and the optical spec-

troscopy techniques used to reveal the exciton physics in ML TMD materials are introduced in the remainder of Sec. [I.](#page-2-0) Neutral exciton binding energies and their impact on light-matter coupling effects are discussed in Sec. [II.](#page-7-0) Exciton physics at higher densities and in the presence of free carriers are described in Sec. [III.](#page-17-1) Finally, the impact of the Coulomb interaction and external fields on valley physics is outlined in Sec. [IV,](#page-19-0) and open questions and challenges are addressed throughout the text to stimulate further work on the excitonic properties of atomically thin materials.

A. Basic band structure and optical selection rules

In addition to the strong Coulomb interaction in ML TMDs, the crystal symmetry and orbital character of the bands are responsible for the underlying spin-valley properties and optical selection rules. Bulk TMDs in the semiconducting 2H phase consist of X-M-X building blocks with weak van-der-Waals bonding between the layers and are characterized by the D_{6h} point symmetry group for stoichiometric compounds [\(Ribeiro-Soares](#page-27-6) [et al.](#page-27-6), [2014;](#page-27-6) [Wilson and Yoffe,](#page-28-3) [1969\)](#page-28-3). In bulk TMDs, the indirect band gap corresponds to the transition between the valence band maximum (VBM) at the center of the hexagonal Brillouin zone (Γ point) and the conduction band minimum (CBM) situated nearly half way along the $\Gamma - K$ direction (Yun *[et al.](#page-29-4)*, [2012;](#page-29-3) Zhao *et al.*, [2013b\)](#page-29-4). The electronic states at the Γ point contain contributions from the p_z orbitals of the chalcogen atom and the d_{z^2} orbitals of the transition metal. In contrast, the K^{\pm} point conduction and valence band states at the corners of the hexagonal Brillouin zone are very strongly localized in the metal atom plane, as they are composed of transition metal atom $d_{x^2y^2} \pm id_{xy}$ states (VB) and d_{z^2} states (CB) slightly mixed with the chalcogen $p_x \mp i p_y$ orbitals [\(Kormanyos](#page-25-4) et al., [2015;](#page-25-4) Li [et al.](#page-26-11), [2007;](#page-26-11) Zhu [et al.](#page-29-5), 2011). The spatial overlap between adjacent MX₂ layers of the orbitals corresponding to the Γ point (VB) and the midpoint along $\Gamma - K$ (CB) is considerable. As a result, in progressing from bulk crystals to few layer samples and eventually to monolayers, the indirect gap energy corresponding to the separation between Γ and the midpoint along $\Gamma - K$ increases whereas the K^{\pm} point CB and VB energies are nearly unaffected. In the ML limit, the semiconductor undergoes a crossover from an indirect to a direct gap, the later situated at the K^{\pm} points (see Fig. $1b)^1$ $1b)^1$, and resulting in much stronger light emission for MLs as compared to bulk and bilayers (Mak [et al.](#page-26-3), [2010;](#page-26-3) [Splendiani](#page-27-0) et al., [2010\)](#page-27-0).

As compared with bulk samples, the TMD MLs are described by the lower symmetry D_{3h} point group. The symmetry elements include a horizontal σ_h reflection plane containing the metal atoms, a threefold C_3 rotation axis intersecting the horizontal plane in the center of the hexagon, as well as a S_3 mirror-rotation axis, three twofold C_2 rotation axes lying in the ML plane, and mirror reflection planes σ_v containing the C_2 axes [\(Koster](#page-26-12) *[et al.](#page-26-12)*, [1963\)](#page-26-12). The symmetry of the states at K^{\pm} is still lower and characterized by the C_{3h} point group where only C_3 , S_3 axes and σ_h elements are present.

The spin-orbit interaction in TMDs is much stronger than in graphene, the most prominent 2D material. The origin of this distinction lies simply in the relatively heavy elements in the TMDs and the involvement of the transition metal d orbitals. In monolayer TMDs, the spin splitting at the K point in the valence band is around 200 meV (Mo-based) and 400 meV (W-based) [\(Chei](#page-24-7)[wchanchamnangij and Lambrecht,](#page-24-7) [2012;](#page-24-7) Miwa [et al.](#page-26-13), [2015;](#page-26-13) Xiao [et al.](#page-28-6), [2012;](#page-28-6) [Zhang](#page-29-2) et al., [2014b;](#page-29-2) Zhu [et al.](#page-29-5), [2011\)](#page-29-5). This coupling gives rise to the two valence subbands and, accordingly, to two types of excitons, A and B, which involve holes from the upper and lower energy spin states, respectively. At the CBM, a smaller, but significant spin splitting is also expected due to partial compensation of the p - and d -states contributions [\(Ko](#page-25-4)[rmanyos](#page-25-4) et al., [2015;](#page-25-4) Kormányos et al., [2014;](#page-25-5) [Kosmider](#page-26-7) [et al.](#page-26-7), [2013;](#page-26-7) Liu [et al.](#page-26-14), [2013\)](#page-26-14). Interestingly, depending on the metal atom (Mo or W), the conduction band spin splitting has a different sign, as indicated in Fig. [1c](#page-5-1),d. Hence, at the K point, the spin degeneracy of both the conduction and valence bands is fully lifted. This stands in marked contrast to typical GaAs or CdTe quantumwell structures where the CBM and VBM occur at the Γ point and both the conduction and valence band states remain spin degenerate. The CB spin splitting results in an energy separation between the spin-allowed and optically active (bright) transitions and the spin-forbidden and optically inactive transitions (dark). The exact amplitude of the splitting for exciton states will also depend on the contribution from the electron-hole Coulomb exchange energy [\(Dery and Song,](#page-25-6) [2015;](#page-25-6) [Echeverry](#page-25-7) et al., [2016;](#page-25-7) Qiu [et al.](#page-27-7), [2015\)](#page-27-7). The lowest energy transition in $MoX₂$ is expected to be the bright exciton [\(Kosmider](#page-26-7) [et al.](#page-26-7), [2013;](#page-26-7) Liu [et al.](#page-26-14), [2013\)](#page-26-14), which is consistent with temperature dependent PL measurements [\(Wang](#page-28-9) et al., [2015;](#page-28-9) [Zhang](#page-29-6) et al., [2015d\)](#page-29-6), although recent studies discuss the possibility of the ground state in ML $MoX₂$ being dark [\(Baranowski](#page-24-11) et al., [2017;](#page-24-11) [Molas](#page-26-15) et al., [2017\)](#page-26-15). In contrast for the WX_2 materials, dark excitons are predicted to be lower energies, in agreement with temperature dependent studies [\(Arora](#page-24-12) et al., [2015a;](#page-24-12) [Wang](#page-28-9) et al., [2015;](#page-28-9) [Withers](#page-28-10) et al., [2015;](#page-28-10) [Zhang](#page-29-6) et al., [2015d\)](#page-29-6), measurements in transverse magnetic fields [\(Molas](#page-26-15) et al., [2017;](#page-26-15) [Zhang](#page-29-7) [et al.](#page-29-7), [2017\)](#page-29-7) and experiments probing excitons with outof-plane dipole moments [\(Wang](#page-28-11) et al., [2017;](#page-28-11) [Zhou](#page-29-8) et al., [2017\)](#page-29-8).

The chiral optical selection rules for interband transitions in the K^{\pm} valleys can be deduced from symmetry arguments: The orbital Bloch functions of the VB

 1 We note that here and in the following original figures are reproduced without changes in the same format as presented in their respective source publications.

FIG. 1 (a) Monolayer transition metal dichalcogenide crystal structure. The transition metal atoms appear in black, the chalcogen atoms in yellow. (b) Typical band structure for MX² monolayers calculated using Density Functional Theory (DFT) and showing the quasiparticle band gap E_g at the K points and the spin-orbit splitting in the valence band [\(Ramasubramaniam,](#page-27-5) [2012\)](#page-27-5). (c) Schematic in a single-particle picture showing that the order of the conduction bands is opposite in MoX₂ and WX₂ monolayers [\(Kormanyos](#page-25-4) *et al.*, [2015\)](#page-25-4). The contribution from Coulomb exchange effects that has to be added to calculate the separation between optically active (bright - spin allowed) and optically inactive (dark - spin forbidden) excitons is not shown [\(Echeverry](#page-25-7) et al., [2016\)](#page-25-7)

states at K^{\pm} points are invariants, while the CB states transform like the states with angular momentum components of ± 1 , i.e., according to the E_1/E_2 irreducible representations of the C_{3h} point group. Therefore, the optical selection rules for the interband transitions at K^{\pm} valleys are chiral: the σ^{+} (σ^{-}) circularly polarized light can only couple to the transition at K^+ (K^-) [\(Cao](#page-24-6) [et al.](#page-24-6), [2012;](#page-24-6) Mak [et al.](#page-26-16), [2012;](#page-26-16) [Sallen](#page-27-8) et al., [2012;](#page-27-8) [Xiao](#page-28-6) [et al.](#page-28-6), [2012;](#page-28-6) Yao [et al.](#page-28-12), [2008;](#page-28-12) Zeng [et al.](#page-29-9), [2012\)](#page-29-9). This permits the optical generation and detection of the spinvalley polarization, rendering the TMD monolayers an ideal platform to study the electron valley degree of freedom in the context of valleytronics [\(Behnia,](#page-24-13) [2012;](#page-24-13) [Rycerz](#page-27-9) [et al.](#page-27-9), [2007;](#page-27-9) [Schaibley](#page-27-10) et al., [2016;](#page-27-10) Xiao [et al.](#page-28-13), [2007\)](#page-28-13). In that context, it is important to emphasize, that for an electron to change valley, it has either to flip its spin (see Fig. [1c](#page-5-1),d) or undergo an energetically unfavorable transition, especially for the valence states. As a result, optically generated electrons and holes are both valley and spin polarized, which is termed spin-valley locking. Therefore, following the σ^+ excitation, the exciton emission in TMD MLs can be co-polarized with the laser if the valley polarization lifetime is longer or of the order of the recombination time. This behavior stands in contrast to that of III-V or II-VI quantum wells where excitation

with the circularly polarized light usually results only in spin-polarization of the charge carriers [\(Dyakonov,](#page-25-8) [2008\)](#page-25-8).

B. Brief survey of monolayer characterization and optical spectroscopy techniques

Before describing the exciton physics in detail, we summarize some relevant practical information about ML TMD samples and their typical environment (substrates) and describe the basic techniques used to investigate the optical properties. Monolayer TMDs can be obtained by the mechanical exfoliation [\(Frindt,](#page-25-1) [1966;](#page-25-1) [Novoselov](#page-26-2) et al., [2005\)](#page-26-2), chemical exfoliation [\(Coleman](#page-25-9) [et al.](#page-25-9), [2011;](#page-25-9) [Joensen](#page-25-2) et al., [1986;](#page-25-2) [Smith](#page-27-11) et al., [2011\)](#page-27-11), or CVD (Liu [et al.](#page-26-17), [2012;](#page-26-17) [Najmaei](#page-26-18) et al., [2013;](#page-26-18) [van der](#page-29-10) [Zande](#page-29-10) et al., [2013\)](#page-29-10) and van-der-Waals epitaxy growth (Liu [et al.](#page-26-19), [2015a;](#page-26-19) [Xenogiannopoulou](#page-28-4) et al., [2015;](#page-28-4) [Zhang](#page-29-2) [et al.](#page-29-2), [2014b\)](#page-29-2). Mechanical exfoliation is a convenient method to produce high-quality monolayer flakes from bulk crystals. Controlled growth of large-area monolayer material on different substrates using CVD or van-der-Waals epitaxy is a very active area of research and samples with high crystal quality have been already obtained.

Following isolation of a ML by micromechanical cleavage, the flakes can be deposited onto several kinds of sub-

FIG. 2 (a) Schematic real-space representation of the electron-hole pair bound in a Wannier-Mott exciton, showing the strong spatial correlation of the two constituents. The arrow indicates the center of mass wavevector responsible for the motion of the exciton as a whole. (b) Illustration of a typical exciton wavefunction calculated for monolayer MoS₂ from (Qiu [et al.](#page-27-4), [2013\)](#page-27-4). The modulus squared of the electron wavefunction is plotted in color scale (gray scale) for the hole position fixed at the origin. The inset shows the corresponding wavefunction in momentum space across the Brillouin zone, including both K^+ and K^- exciton states. (c) Representation of the exciton in reciprocal space, with the contributions of the electron and hole quasiparticles in the conduction (CB) and valence (VB) bands, respectively, shown schematically by the width of the shaded area. (d) Schematic illustration of the optical absorption of an ideal 2D semiconductor including the series of bright exciton transitions below the renormalized quasiparticle band gap. In addition, the Coulomb interaction leads to the enhancement of the continuum absorption in the energy range exceeding E_B , the exciton binding energy. The inset shows the atom-like energy level scheme of the exciton states, designated by their principal quantum number n, with the binding energy of the exciton ground state $(n = 1)$ denoted by E_B below the free particle bandgap (FP)

strates, SiO_2/Si , fused silica, sapphire, etc. SiO_2/Si substrates are widely used as (i) SiO₂ can help to optimize the contrast for monolayers in optical microscopy during mechanical exfoliation (Lien *[et al.](#page-26-20)*, [2015\)](#page-26-20), and (ii) they are compatible with microelectronics standards [\(Radis](#page-27-12)[avljevic](#page-27-12) et al., [2011a\)](#page-27-12). Encapsulation of ML flakes in hexagonal boron nitride, a layered material with a band gap in the deep UV [\(Taniguchi and Watanabe,](#page-28-14) [2007\)](#page-28-14), has been shown to enhance the sharpness of the optical transitions in ML TMDs, particularly at low temperatures [\(Ajayi](#page-24-14) et al., [2017;](#page-24-14) [Cadiz](#page-24-15) et al., [2017;](#page-24-15) [Chow](#page-25-10) [et al.](#page-25-10), [2017;](#page-25-10) Jin [et al.](#page-25-11), [2016;](#page-25-11) [Manca](#page-26-21) et al., [2017;](#page-26-21) [Tran](#page-28-15) [et al.](#page-28-15), [2017;](#page-28-15) [Wang](#page-28-16) et al., [2017;](#page-28-16) Zhou [et al.](#page-29-8), [2017\)](#page-29-8). This improvement is attributed to a reduction in detrimental surface and environmental effects on the samples. In addition to simple optical contrast (differential reflectivity) measurements, Raman spectroscopy is often used to determine the number of layers of TMDs flakes [\(Korn](#page-26-22) [et al.](#page-26-22), [2011;](#page-26-22) [Tonndorf](#page-28-17) et al., [2013\)](#page-28-17). The energy spacing between two high-frequency phonon modes A_{1g} and E_{2g}^1 can be used to identify thickness of exfoliated molybdenum dichalcogenides MX_2 when it is thinner than 5 layers [\(Zhang](#page-29-11) et al., [2015b\)](#page-29-11). As only the monolayer is a directgap semiconductor (with the possible exception of $MoTe₂$ bilayers), analyzing the intensity and emission energy of photoluminescence (PL) signals allows identifying monolayer flakes. However, as the PL emission tends to favor low-energy states, including possible defect and impurity sites, care must be taken in applying this approach, especially at low temperatures. As an alternative, optical

reflection and transmission spectroscopy can be used to identify the number of layers by quantitatively measuring the strength of the optical response. (Mak [et al.](#page-26-3), [2010;](#page-26-3) Zhao [et al.](#page-29-12), [2013a\)](#page-29-12)

II. COULOMB BOUND ELECTRON-HOLE PAIRS

In this section we summarize the main properties of the exciton states in TMD monolayers and discuss their importance for the optical response in terms of their energies (exciton resonances) and oscillator strengths (optically bright versus dark states). We start with a brief introduction of the electron and hole quasi-particle states forming the excitons at the fundamental band gap. Then, we discuss the consequences of the Coulomb interaction, including direct and exchange contributions, followed by an overview of exciton binding energies and light-matter coupling in monolayer TMDs.

The promotion of an electron from the filled valence band to the empty conduction band leaves an empty electron state in the valence band. The description of such a many-body system can be reduced to the two-particle problem of the negatively charged conduction electron interacting with a positively charged valence hole. The hole Bloch function $|h\rangle = |s_h, \tau_h, \mathbf{k}_h\rangle$ is derived from the Bloch function of the empty electron state $|v\rangle = |s_v, \tau_v, \mathbf{k}_v\rangle$ in the valence band by applying the time-reversal operator $|h\rangle = \mathcal{K}|v\rangle$ [\(Bir and Pikus,](#page-24-16) [1974\)](#page-24-16). Here, s_{ν} ($\nu = c, v$) represent the spin index, $\tau_{\nu} = \pm 1$ is the valley index, and k_{ν} is the wave vector for a conduction (c) or valence (v) state. As the time reversal operator changes the orbital part of the wavefunction to its complex conjugate and also flips the spin, the hole wavevector is opposite that of the empty electron state, i.e., $k_h = -k_v$, the hole valley (and spin) quantum numbers are opposite to those of the empty electron state as well: $s_h = -s_v$, $\tau_h = -\tau_v$. This transformation is natural to describe the formation of the electron-hole pair from the photon with a given polarization. In case of TMD monolayers, a σ^+ photon with a wavevector projection q_{\parallel} to the plane of the layer creates an electron with a wavevector k_e in the $s_e = +1/2$ state in $\tau_e = +1$ (K⁺) valley, leaving a state with wavevector $k_v = k_e - q_{\parallel}$ in the valence band unoccupied. As a result, the corresponding hole wavevector is $k_h = -k_v = q_{\parallel} - k_e$, with the center of mass wavevector of the electron-hole pair equal to $\mathbf{K}_{\text{exc}} = \mathbf{k}_e + \mathbf{k}_h = \mathbf{q}_{\parallel}$, as expected for the quasiparticle created by a photon. Accordingly, the hole valley index, $\tau_h = -1$, and spin, $s_h = -1/2$, are formally opposite to those of the conduction-band electron. In a similar manner, the absorption of σ^- photon results in the formation of the electron-hole pair with $\tau_e = -\tau_h = -1, s_e = -s_h = -1/2$ [\(Glazov](#page-25-12) *et al.*, [2014,](#page-25-12) [2015\)](#page-25-13).

A. Neutral excitons: direct and exchange Coulomb interaction

To discuss the consequences of the Coulomb electronhole interaction we separate the *direct* and *exchange* contributions, both further including long-range and shortrange interactions, with certain analogies to traditional quasi-2D quantum well excitons [\(Dyakonov,](#page-25-8) [2008\)](#page-25-8). The long-range part represents the Coulomb interaction acting at inter-particle distances in real space larger than the inter-atomic bond lengths (i.e., for small wavevectors in reciprocal space compared to the size of the Brillouin zone). In contrast, the *short-range* contribution originates from the overlap of the electron and hole wavefunctions at the scales on the order of the lattice constant ($a_0 \approx 0.33$ nm in ML WSe₂), typically within one or several unit cells (i.e., large wavevectors in reciprocal space).

The direct Coulomb interaction describes the interaction of positive and negative charge distributions related to the electron and the hole. The long-range part of the direct interaction is determined mainly by the envelope function of the electron-hole pair being only weakly sensitive to the particular form of the Bloch functions, i.e., valley and spin states; it rather depends on the dimensionality and dielectric properties of the system. It has an electrostatic origin and provides the dominant contribution to the exciton binding energy, E_B , see Sec. [II.B.](#page-10-0) The short-range part of the direct interaction stems from the Coulomb attraction of the electron and the hole within the same or neighboring unit cells. It is sensitive to the particular form of the Bloch functions and is, as a rule, considered together with the corresponding part of the exchange interaction. In a semi-classical picture, the long-range direct interaction thus corresponds to attractive Coulomb forces between opposite charges. As a consequence, an electron and a hole can form a bound state, the neutral exciton, with strongly correlated relative positions of the two constituents in real space, as schematically shown in Fig. [2a](#page-6-0). The concept of correlated electron-hole motion is further illustrated in Fig. [2b](#page-6-0), as reproduced from Ref. (Qiu *[et al.](#page-27-4)*, [2013\)](#page-27-4), where the modulus squared of the electron wavefunction relative to the position of the hole is presented for the case of the exciton ground state in monolayer $MoS₂$. In TMD MLs, the exciton Bohr radius is on the order of one to a few nanometers and the correlation between an electron and a hole extends over several lattice periods. Thus, strictly speaking, the exciton could be formally understood to be of an intermediate nature between the so-called Wannier-Mott or large-radius type similar to prototypical semiconductors such as GaAs and $Cu₂O$ and Frenkel exciton, which corresponds to the charge transfer between nearest lattice sites. However, to describe the majority of the experimental observations, the Wannier-Mott description in the effective mass approximation appears to be largely appropriate even for quantitative predictions.

In the k-space, the exciton wavefunction Ψ^X can be

presented as [\(Bir and Pikus,](#page-24-16) [1974;](#page-24-16) [Glazov](#page-25-13) et al., [2015\)](#page-25-13)

$$
\Psi^X = \sum_{e,h} C^X(\mathbf{k}_e, \mathbf{k}_h) |e; h\rangle, \tag{1}
$$

where the correlation of the electron and hole in the exciton is described by a coherent, i.e., phase-locked, superposition of electron and hole states $(|e\rangle = |s_e, \tau_e, \mathbf{k}_e\rangle$ and $|h\rangle = |s_h, \tau_h, \mathbf{k}_h\rangle$ around the respective extrema of the bands. Relative contributions of these states to the exciton are described by the expansion coefficients C^X , which are usually determined from the effective two-particle Schrödinger or Bethe-Salpeter equation. Their values are schematically represented by the size of the filled area in Fig. [2c](#page-6-0), with the results of an explicit calculation shown in the inset of Fig. [2b](#page-6-0) for electrons in monolayer $MoS₂$. As a consequence of the large binding energy of excitons and their small Bohr radius in real-space $(a_B \simeq 1 \text{ nm}),$ the spread of the exciton in k -space is significant. Therefore states further away from the K -point band extrema (see inset in Fig. 2b) are included in the exciton wavefunction (Qiu [et al.](#page-27-4), [2013;](#page-27-4) [Wang](#page-28-18) et al., [2015\)](#page-28-18).

As previously noted, the correlation represented in Eq. (1) is strictly related to the relative motion of the carriers. In contrast, the exciton center-of-mass can propagate freely in the plane of the material, in accordance with the Bloch theorem. The resulting exciton states $X = \{K_{\text{exc}}, s_e, \tau_e, s_h, \tau_h, (n, m)\}\$ are labeled by the center-of-mass wavevector K_{exc} , electron and hole spin and valley indices, s_e , τ_e , s_h , τ_h and the relative motion labels (n, m) . The relative motion states can be labelled by the principal and magnetic quantum number as (n, m) , with $n = 1, 2, 3...$ a natural number, $m \in \mathbb{Z}$ and $|m| < n$. To choose a notation similar to the hydrogen atom for s, p, d states, we use here $(n, 0) = ns$ where $n \in \mathbb{N}$ and $(n, \pm 1) = (np, \pm 1)$ for $n > 1$, $(n, \pm 2) = (nd, \pm 2)$ for $n > 2$ etc; the precise symmetry of excitonic states is discussed below in Sec. [II.C.](#page-14-0)

In particular, the principal quantum number n is the primary determinant of the respective binding energy, with the resulting series of the ground state $(n = 1)$ and excited states $(n > 1)$ of Wannier-Mott excitons roughly resembling the physics of the hydrogen atom, as represented by the energy level scheme in Fig. [2d](#page-6-0). The selection rules for optical transitions are determined by the symmetry of the excitonic wavefunctions, particularly, by the set of the spin and valley indices $s_{e,h}$ and $\tau_{e,h}$ and the magnetic quantum number m . These quantities are of particular importance for the subdivision of the excitons into so-called bright states, or optically active, and dark states, i.e., forbidden in single-photon absorption process, as further discussed in the following sections.

In addition to the formation of excitons, a closely related consequence of the Coulomb interaction is the socalled self-energy contribution to the absolute energies of electron and hole quasiparticles. In a simplified picture, the self energy is related to the repulsive interaction between identical charges and leads to an overall increase of the quasiparticle band gap of a semiconductor, i.e., the energy necessary to create an unbound electron-hole pair in the continuum, referred to as 'free-particle (or quasiparticle) band gap'. In many semiconductors, including TMD monolayers, the self-energy contribution and the exciton binding energy are found to be almost equal, but of opposite sign. Thus, the two contributions tend to cancel one another out with respect to the absolute energies.

Nevertheless, these interactions are of central importance as they determine the nature of the electronic excitations and the resulting properties of the material. To demonstrate the later, a schematic illustration of the optical absorption in an ideal 2D semiconductor is presented in Fig. [2d](#page-6-0). The changes associated with the presence of strong Coulomb interactions result in the formation of the exciton resonances below the renormalized free-particle band gap. Importantly, the so-called optical band gap is then defined with respect to the lowest energy feature in absorption, i.e., the ground state of the exciton $(n = 1)$. The optical gap thus differs from free-particle band gap, which corresponds, as previously introduced, to the onset of the continuum of unbound electrons and holes. The free particle bandgap is thus formally equivalent to the $n = \infty$ limit of the bound exciton state. Consequently, samples with different exciton binding energies and free particle bandgaps can have optical bandgaps at very similar energies. This can be illustrated, e.g., in comparative studies of the absolute energies of exciton resonances for monolayer samples placed in different dielectric environments, effectively tuning both the exciton binding energy and the free particle bandgap [\(Cadiz](#page-24-15) [et al.](#page-24-15), [2017;](#page-24-15) Raja [et al.](#page-27-13), [2017;](#page-27-13) Stier [et al.](#page-28-19), [2016b\)](#page-28-19). As a final point, the Coulomb interaction leads to a significant enhancement of the continuum absorption, which is predicted to extend many times of E_B into the band [\(Haug](#page-25-14) [and Koch,](#page-25-14) [2009;](#page-25-14) [Shinada and Sugano,](#page-27-14) [1966\)](#page-27-14).

In comparison to the *direct* coupling part of the Coulomb interaction, the exchange contribution denotes the Coulomb interaction combined with the Pauli exclusion principle. The latter is a well-known consequence of the fact that both types of quasiparticles (electrons and holes) result from a sea of indistinguishable charged fermions occupying filled bands: The wavefunction of the many-electron system with one carrier promoted to the conduction band should be antisymmetrized with respect to permutations of the particles. Hence, just as for exchange interaction in atoms, the energy of exciton depends on the mutual orientation of electron and hole spins and, as a particular feature of the TMD MLs, on the quasi-particle valley states. In analogy to the direct coupling, the Coulomb exchange interaction can be also separated into the long-range and the short-range parts. In particular, the long-range exchange interaction is of electrodynamic nature, in close analogy to the exchange interaction between an electron and a positron [\(Berestet](#page-24-17)[skii and Landau,](#page-24-17) [1949\)](#page-24-17). It can be thus interpreted as a result of interaction of an exciton with the induced electromagnetic field in the process of virtual electron-

TABLE I Impact of different types of electron-hole interaction on optical and polarization properties of excitons in TMD MLs.

Coulomb term	Impact			
Direct	Exciton binding energy			
	neutral excitons \sim 500 meV			
	charged excitons, biexcitons ~ 50 meV			
	Quasi-particle bandgap			
	self-energy ~ 500 meV			
Exchange	Exciton fine structure			
long-range	neutral exciton spin/valley depolarization			
	~ 110 meV			
short-range	splitting of dark and bright excitons			
	\sim 10's of meV			

hole recombination [\(Bir and Pikus,](#page-24-16) [1974;](#page-24-16) [Denisov and](#page-25-15) [Makarov,](#page-25-15) [1973;](#page-25-15) [Goupalov](#page-25-16) et al., [1998\)](#page-25-16): The bright exciton can be considered as a microscopic dipole which produces an electric field, the back-action of this field on the exciton is the long-range electron-hole exchange interaction. On a formal level, it corresponds to the decomposition of the Coulomb interaction up to the dipole term and calculation of its matrix element on the antisymmetrized Bloch functions [\(Andreani,](#page-24-18) [1995\)](#page-24-18). In TMD monolayers, the *long-range* exchange part, being much larger than for III-V or II-VI quantum wells, facilitates transitions between individual exciton states excited by the light of different helicity, thus mainly determining the spin-valley relaxation of the excitons, see Sec. [IV.](#page-19-0) At short-range, Pauli exclusion causes the exchange interaction to depend strongly on the spin and valley states of the particles. It thus contributes to the total energies of the many-particle complexes, depending on the spin and valley states of the individual constituents and impacts the separation between optically dark and bright excitons [\(Echeverry](#page-25-7) et al., [2016;](#page-25-7) Qiu [et al.](#page-27-7), [2015\)](#page-27-7). Among typical examples are the so-called triplet and singlet exciton states (i.e., the exciton fine structure) corresponding to parallel and anti-parallel alignment of the electron and hole spins, respectively. Lacking a classical analog, the exchange interaction is a more subtle contribution compared to the direct Coulomb interaction. A rough estimate of the exchange to direct interaction ratio in exciton is provided by the ratio of the binding energy, E_B , and the band gap, E_g : ~ E_B/E_g [\(Bir and Pikus,](#page-24-16) [1974\)](#page-24-16). As it is summarized in Table [I,](#page-9-0) the overall ratio of the direct and exchange contributions in TMDs is on the order of 10 : 1, depending, in particular, on the exciton wavevector for the long-range interaction [\(Glazov](#page-25-12) et al., [2014\)](#page-25-12). Nevertheless, as it is discussed in the following sections, the consequences of exchange interaction are of central importance in understanding many-particle electronic excitations in TMD monolayers.

One of the distinct properties of TMD monolayers is the unusually strong long-range Coulomb interaction and its unconventional interparticle distance dependence, leading to large exciton binding energies and band-gap renormalization effects. First, the decrease of dimensionality results in smaller effective electron and hole separations, particularly, perpendicular to the ML plane, where the wavefunctions of the electron and hole occupy only several angstroms as compared to tens of nanometers in bulk semiconductors. In the simple hydrogenic model, this effect yields to a well-known four-fold increase in exciton binding energy in 2D compared to 3D [\(Ivchenko,](#page-25-17) [2005\)](#page-25-17). Second, the effective masses in the K^{\pm} valleys of the electron, m_e , and hole, m_h , in TMD MLs are relatively large, on the order of $\sim 0.5 m_0$, with m_0 denoting the free electron mass [\(Kormanyos](#page-25-4) $et \ al.,\ 2015;\ Liu \ et \ al.,\ 2013).$ $et \ al.,\ 2015;\ Liu \ et \ al.,\ 2013).$ $et \ al.,\ 2015;\ Liu \ et \ al.,\ 2013).$ $et \ al.,\ 2015;\ Liu \ et \ al.,\ 2013).$ $et \ al.,\ 2015;\ Liu \ et \ al.,\ 2013).$ Hence, the reduced mass $\mu = m_e m_h/(m_e + m_h) \approx 0.25$ m_0 is also larger compared to prominent semiconductor counterparts such as GaAs ($\mu \approx 0.06$ m₀). Finally, in TMD MLs, the material is generally surrounded by air/vacuum (or dielectrics with relatively small permitivity). This reduces dielectric screening of the Coulomb interaction, since the electric field produced by the electron-hole pair is present largely outside of the ML itself. These features of the screening also result in a substantial deviation of the electron-hole interaction from the conventional $1/r$ distance dependence, as discussed in detail in Sec. [II.B.2.](#page-12-0) Nevertheless, one can still estimate the impact of the dimensionality, the effective mass, and the reduced screening on the exciton binding energy E_B within the framework of the 2D hydrogen-like model: $E_B \propto 4Ry \mu/(m_0 \varepsilon_{\text{eff}}^2)$, where Ry is the Rydberg constant of 13.6 eV and ε_{eff} is a typical effective dielectric constant of the system, roughly averaged from the contributions of the ML and the surroundings, m_0 is the free electron mass. Clearly, an increase in μ and decrease in ε_{eff} result in the increase of the binding energy. As an example, this simple expression provides a binding energy on the order of 0.5 eV for realistic parameters of $\mu = 0.25$ m_0 and $\varepsilon_{\text{eff}} = 5$.

As a final step in introducing the Coulomb terms and their role in the physics of TMD monolayers, we can formally identify the direct and exchange terms in the effective exciton Hamiltonian in k -space in the two-band approximation:

$$
\mathcal{H}_{XX'}(\mathbf{k}_e, \mathbf{k}_h; \mathbf{k}'_e, \mathbf{k}'_h) =
$$
\n
$$
\left[\mathcal{H}_e(\mathbf{k}_e) \delta_{\mathbf{k}_e, \mathbf{k}'_e} + \mathcal{H}_h(\mathbf{k}_h) \delta_{\mathbf{k}_h, \mathbf{k}'_h} + V_{\mathbf{k}_e, \mathbf{k}_h, \mathbf{k}'_e, \mathbf{k}'_h} \right] \delta_{XX'} +
$$
\n
$$
U_{\mathbf{k}_e, \mathbf{k}_h; \mathbf{k}'_e, \mathbf{k}'_h} (EH; E'H') \delta_{\mathbf{K}, \mathbf{K}'}, \quad (2)
$$

where $\mathcal{H}_e(\mathbf{k}_e)$ $(\mathcal{H}_h(\mathbf{k}_h))$ are the electron (hole) singleparticle Hamiltonians, $V_{\mathbf{k}_e \mathbf{k}_h; \mathbf{k}'_e, \mathbf{k}'_h}$ stands for the matrix element of the direct (long-range) Coulomb interaction between the electron and the hole, and $U_{\mathbf{k}_e \mathbf{k}_h; \mathbf{k}'_e, \mathbf{k}'_h} (EH; E'H')$ is the matrix of the electron-hole exchange interaction. Here $E = s_e \tau_e$, $H = s_h \tau_h$ are the electron and hole spin and valley indices, the dependence of the single-particle Hamiltonians on E and H is implicitly assumed. The last term comprises the short- and long-range contributions to the electron-hole exchange interaction. In real space, the second line of Eq. [\(2\)](#page-9-1) corresponds to the standard exciton Hamiltonian in the effective mass approximation with a properly screened Coulomb interaction potential with the additional shortrange part in the form $V_0(EH; E'H')\delta(\mathbf{r}_e - \mathbf{r}_h)$ with the parameters $V_0(EH; E'H')$ determined by particular form of the Bloch functions [\(Bir and Pikus,](#page-24-16) [1974\)](#page-24-16).

B. Exciton binding energy

1. Exciton and continuum states in optics and transport

To determine the exciton binding energy E_B directly by experiment, one must identify both the absolute energy position of the exciton resonance E_X and that of the free-particle bandgap E_q to obtain $E_B = E_q - E_X$. For this purpose, several distinct techniques have been successfully applied to TMD monolayers. The transition energy $E_X^{(n=1)}$ of the exciton ground state can be readily obtained using optical methods. Due to the strong lightmatter coupling (cf. Sec. [II.C\)](#page-14-0) the excitons appear as pronounced resonances centered at photon energies corresponding to $E_X^{(n=1)}$ in optical absorption, reflectance, photoluminescence (PL), photoluminescence excitation (PLE), and photocurrent (PC) measurements. In case of PL, room-temperature measurements are usually preferred to avoid potential contributions from defect states. As an example, PL spectra of MoSe₂ monolayer from Ref. [\(Ugeda](#page-28-20) et al., [2014\)](#page-28-20) are presented in the left panel of Fig. [3a](#page-11-0), illustrating the strong emission from the groundstate exciton transition.

In contrast, the precise determination of the freeparticle bandgap energy is more challenging problem and a recurring one for semiconductors with large exciton binding energies where strong exciton resonances may mask the onset of a continuum of states. A direct approach is provided by the scanning tunneling spectroscopy (STS), which measures tunneling currents as a function of the bias voltage through a tip positioned in close proximity to the sample. Such measurements can probe the electronic density of states in the vicinity of the band gap, mapping energy levels of free electrons in both the valence and conduction bands. A typical STS spectrum for a MoSe₂ monolayer supported by bilayer of graphene [\(Ugeda](#page-28-20) et al., [2014\)](#page-28-20) is presented in the right panel of Fig. [3a](#page-11-0). As a function of tip voltage relative to the sample, a region of negligible tunneling current is observed. This arises from the band gap where no electronic states are accessible. The lower and upper onset of the tunnel current correspond to the highest occupied electron states at the VBM and the lowest unoccupied states at the CBM, respectively. The size of the bandgap E_q is extracted from the difference between these onsets. As previously discussed, the exciton binding energy is then directly obtained from the difference between E_g measured by STS and the exciton transition energy $E_X^{(n=1)}$

identified in the optical spectroscopy (compare right and left panel in Fig. [3a](#page-11-0)). The reported values, as summa-rized in the Table [II,](#page-13-0) range from 0.22 eV for MoS_2 [\(Zhang](#page-29-13) *[et al.](#page-29-13)*, [2014a\)](#page-29-13) to 0.55 eV for MoSe₂ [\(Ugeda](#page-28-20) *et al.*, [2014\)](#page-28-20); further reports include [\(Bradley](#page-24-19) et al., [2015;](#page-24-19) Chiu [et al.](#page-24-20), [2015;](#page-24-20) [Rigosi](#page-27-15) *et al.*, [2016;](#page-27-15) [Zhang](#page-29-14) *et al.*, [2015a\)](#page-29-14). The differences can be related to (i) the overall precision in extracting the onsets of the tunneling current and (ii) to the use of different conducting substrates required for the STS, i.e., the influence of different dielectric environments and related proximity effects. In addition, the complexities of the band structure of the TMDs, with several valley extrema being relatively close in energy (see Sec. [I.A\)](#page-4-0) were shown to be of particular importance for the identification of the bands contributing to the initial rise in the tunneling current [\(Zhang](#page-29-14) *et al.*, [2015a\)](#page-29-14).

As discussed in Sec. [II.A](#page-7-1) (see Fig. [2d](#page-6-0)), the onset of the free-particle continuum in the absorption spectra is merged with the series of excited exciton states $(n = 2, 3, ...)$, precluding a direct extraction of the bandgap energy in most optical spectroscopy experiments. However, the identification of the series of excited exciton states permits an extrapolation to the expected band gap or for the determination of the band gap through the application of suitable models. These methods are analogous to the measurements of the Rydberg (binding) energy of the hydrogen atom from spectral lines from transitions between different electron states. For an ideal 2D system the exciton energies evolve as $E_B^n = \mu e^4 / [2\hbar^2 \varepsilon_{\text{eff}}^2 (n - 1/2)^2]$ in a hydrogenic series with $n = 1, 2...$ [\(Klingshirn,](#page-25-18) [2007;](#page-25-18) [Shinada and Sugano,](#page-27-14) [1966\)](#page-27-14). As clearly shown in reflection spectroscopy [\(Chernikov](#page-24-8) [et al.](#page-25-3), [2014;](#page-24-8) He et al., [2014\)](#page-25-3), the exciton states in ML $WSe₂$ and $WS₂$, for example, deviate from this simple dependence, see Fig. [3b](#page-11-0). The main reason for the change in the spectrum is the nonlocal dielectric screening associated with the inhomogeneous dielectric environment of the TMD ML. This results in a screened Coulomb potential [\(Cudazzo](#page-25-19) et al., [2011;](#page-25-19) [Keldysh,](#page-25-20) [1979;](#page-25-20) [Rytova,](#page-27-16) [1967\)](#page-27-16) with a distance dependence that deviates strongly from the usual $1/r$ form, as detailed below, and also introduced in the context of carbon nanotubes [\(Adamyan](#page-24-21) [et al.](#page-24-21), [2008;](#page-24-21) [Ando,](#page-24-22) [2010;](#page-24-22) [Deslippe](#page-25-21) et al., [2009;](#page-25-21) [Wang](#page-28-21) [et al.](#page-28-21), [2005\)](#page-28-21).

The energies of the excited states of the excitons $n > 1$ can be directly obtained from linear absorption or reflectance spectroscopy. These states are usually identified by their decreasing spectral weight (oscillator strength) and relative energy separations with increasing photon energies. The oscillator strength for an ideal 2D system is given by $f_n = f_{n=1}/(2n-1)^3$ [\(Shinada and Sug](#page-27-14)[ano,](#page-27-14) [1966\)](#page-27-14). As an example, consider the reflectance contrast spectrum (i.e., the difference of the reflectity of the sample and substrate divided by the substrate reflectivity) from a WS_2 monolayer [\(Chernikov](#page-24-8) et al., [2014\)](#page-24-8), measured at cryogenic temperatures. The spectrum, presented after taking a derivative with respect to photon energy to highlight the features in the left

FIG. 3 Presentation of commonly used experimental techniques to determine exciton binding energies in TMD monolayers. (a) Direct measurement of the free-particle bandgap energy using scanning tunneling spectroscopy of ML MoSe₂ on bilayer graphene (right panel) combined with a measurement of the absolute energy of the exciton ground state from photolumi-nescence (left panel) [\(Ugeda](#page-28-20) *et al.*, [2014\)](#page-28-20). (b) Exciton states of ML WS₂ on an SiO_2/Si substrate from reflectance contrast measurements [\(Chernikov](#page-24-8) et al., [2014\)](#page-24-8). The extracted transition energies of the states and the inferred band-gap position are presented in the right panel. (c) The linear absorption spectrum and the third-order susceptibility extracted from two-photon photoluminescence excitation spectra of ML WSe_2 on fused silica substrate with exciton resonances of the ground and excited states (He [et al.](#page-25-3), [2014\)](#page-25-3). (d) Exciton states as measured by second-harmonic spectroscopy of the A and B transitions in ML WSe₂ [\(Wang](#page-28-7) et al., [2015a\)](#page-28-7). (e) One-photon photoluminescence excitation spectra and the degree of linear polarization of the luminescence of ML WSe₂ with features of excited 2s state of the A and the ground state of the B exciton [\(Wang](#page-28-7) et al., [2015a\)](#page-28-7).

panel of Fig. [3b](#page-11-0), reveals signatures of the excited exciton states. The right panel summarizes the extracted peak energies and the estimated position of the band gap, as obtained directly from the extrapolation of the data and from model calculations. The corresponding exciton binding energy is about 300 meV. Observations of the excited states in reflectance spectra were further re-ported for WSe₂ [\(Arora](#page-24-12) et al., [2015a;](#page-24-12) [Hanbicki](#page-25-22) et al., [2015;](#page-25-22) He [et al.](#page-25-3), [2014\)](#page-25-3) and WS_2 [\(Hanbicki](#page-25-22) et al., 2015; Hill [et al.](#page-25-23), [2015\)](#page-25-23) monolayers, both at cryogenic and room temperature, as well as for $MoSe₂$ [\(Arora](#page-24-23) *et al.*, [2015b\)](#page-24-23). In addition, the relative energy separations between the ground and excited states of the excitons were found to decrease with thickness of multilayer samples [\(Arora](#page-24-12) et al., [2015a;](#page-24-12) [Chernikov](#page-24-8) et al., [2014\)](#page-24-8), reflecting the expected decrease in the binding energy. Similar results were obtained by the related techniques of photoluminescence-excitation spectroscopy (PLE) [\(Hill](#page-25-23) [et al.](#page-25-23), [2015;](#page-25-23) [Wang](#page-28-7) et al., [2015a\)](#page-28-7) and photocurrent (PC) [\(Klots](#page-25-24) et al., [2014\)](#page-25-24) spectroscopy, which also allow identification of the ground and excited-state excitonic transitions. In both cases, this is achieved by tuning the photon

energy of the excitation light source, while the luminescence intensity of a lower-lying emission feature (in PLE) or the current from a sample fabricated into a contacted device (in PC) are recorded. PLE is a multistep process: light is first absorbed, then energy relaxation occurs to the optically-active 1s exciton. As relaxation via phonons plays an important role in TMD MLs [\(Chow](#page-24-24) et al., [2017;](#page-24-24) Molina-Sánchez and Wirtz, [2011\)](#page-26-23), the PLE spectra contain information on both absorption and relaxation pathways. From PLE measurements, excited states of the excitons were observed in WSe_2 [\(Wang](#page-28-7) *et al.*, [2015a\)](#page-28-7), WS_2 (Hill *[et al.](#page-25-23)*, [2015\)](#page-28-18), MoSe₂ [\(Wang](#page-28-18) *et al.*, 2015) and MoS₂ (Hill [et al.](#page-25-23), [2015\)](#page-25-23) monolayers. In PC, the onset of the b andgap absorption in $MoS₂$ monolayers was reported in Ref. [Klots](#page-25-24) et al. [\(2014\)](#page-25-24).

One of the challenges for linear absorption or reflectance spectroscopy, is the dominant response from the exciton ground state, potentially obscuring weaker signatures from the excited states. As an alternative, excited states of the excitons for example $(n, \pm 1) = (np, \pm 1)$ for $n > 1$ can be addressed via two-photon excitation in TMDs [\(Berkelbach](#page-24-25) et al., [2015;](#page-24-25) [Srivastava and](#page-27-17)

[Imamoglu,](#page-27-17) [2015;](#page-27-17) [Wang](#page-28-7) et al., [2015a;](#page-28-7) Ye [et al.](#page-28-22), [2014\)](#page-28-22), while the two-photon absorption by the dipole-allowed transitions for $(n, 0) = 1s, 2s, 3s...$ is strongly suppressed. Indeed, in the standard centrosymmetric model s-shell excitons are allowed in one-photon processes (and forbidden in all processes involving even number of phonons), while *p*-shell excitons are allowed in two-photon processes and forbidden in one-photon processes [\(Mahan,](#page-26-24) [1968\)](#page-26-24). Note that the specific symmetry of the TMD ML can lead to a mixing between exciton s and p-states and activation of p-states in single-photon transitions as well [\(Glazov](#page-25-25) et al., [2017;](#page-25-25) [Gong](#page-25-26) et al., [2017\)](#page-25-26). The mixing is also proposed to originate from a small amount of disorder in the system [\(Berghauser](#page-24-26) et al., [2017\)](#page-24-26)

Here, a commonly used technique is two-photon photoluminescence excitation spectroscopy (2P-PLE). In this method, the (pulsed) excitation source is tuned to half the p exciton transition energy and the resulting luminescence is recorded as a function of the photon excitation energy. Formally, this yields the spectrum of thirdorder nonlinear susceptibility responsible for two-photon absorption. The result of such a 2P-PLE measurement of a WSe₂ monolayer (He *[et al.](#page-25-3)*, [2014\)](#page-25-3) is presented in Fig. [3c](#page-11-0).In contrast to one-photon absorption, the twophoton response is dominated by resonances from the excited exciton states with p-type symmetry, such as the 2p, 3p \ldots states of the A-exciton (labelled A' and A" in Fig. [3c](#page-11-0)). Further reports of the exciton states in 2D TMDs from 2P-PLE include studies of WS_2 (Ye [et al.](#page-28-22), [2014;](#page-28-22) Zhu *[et al.](#page-29-15)*, [2015\)](#page-29-15), WSe_2 [\(Wang](#page-28-7) *et al.*, [2015a\)](#page-28-7) and $MoSe₂ monolayers (Wang et al., 2015).$ Like the analysis of the one-photon spectra, the band gap is extracted either by comparison of the ground and excited state energies with appropriate theoretical models [\(Wang](#page-28-7) et al., [2015a;](#page-28-7) Ye [et al.](#page-28-22), [2014\)](#page-28-22) or from the estimated onset of the continuum absorption (free-particle gap) (He [et al.](#page-25-3), 2014 ; Zhu *[et al.](#page-29-15)*, 2015). In addition to the PLE experiments, both the ground and excited states can be also observed directly in second-harmonic generation spectra, as illustrated in Fig. [3d](#page-11-0) for $WSe₂$ monolayers [\(Wang](#page-28-7) [et al.](#page-28-7), [2015a\)](#page-28-7). The second-harmonic generation takes place because, due to the lack of an inversion center in TMD MLs, the s-shell and p-shell excitons become active both in single- and two-photon processes. This allows for excitation of the given exciton state by two photons and its coherent emission. The microscopic analysis of the selection rules and relative contributions of excitonic states in second-harmonic emission is presented in Ref. [\(Glazov](#page-25-25) et al., [2017\)](#page-25-25), see also [\(Trolle](#page-28-23) et al., [2014\)](#page-28-23). Overall, the main challenge with optical techniques is the correct identification of observed features, made more challenging by a the possible mixture of s and p exci-tons, as well as coupling to phonon modes [\(Chow](#page-25-10) et al., [2017;](#page-25-10) Jin [et al.](#page-25-11), [2016\)](#page-25-11). Topics of current discussion in analyzing different spectra include possible contributions from phonon-assisted absorption, higher-lying states in the band structure, defects, and interference effects.

Further information on exciton states and their energy

can be obtained from measurements of intra-exciton transitions in the mid-IR spectral range after optical injection of finite exciton densities (Cha [et al.](#page-24-27), [2016;](#page-24-27) [Poellmann](#page-27-18) [et al.](#page-27-18), [2015\)](#page-27-18) and measurements of the exciton Bohr radii from diamagnetic shifts at high magnetic fields [\(Stier](#page-28-24) [et al.](#page-28-24), [2016a,](#page-28-24)[b\)](#page-28-19). The latter approach also allows for the estimation of the binding energy of the B-exciton related to the spin-orbit split valence subband. A summary of the exciton binding energies and the corresponding bandgap energies is presented in Table [II.](#page-13-0) While the extracted absolute values vary, largely due to the outlined challenges of precisely determining the absolute position of the band gap, the following observations are compatible with the majority of the literature:

(1) Excitons are tightly bound in TMD monolayers due to the quantum confinement and low dielectric screening, with binding energies on the order of several 100's of meV. The corresponding ground-state Bohr radii are on the order of nanometers and the wavefunction extends over several lattice constants a_0 (for WSe₂ $a_0 \approx$ 0.33 nm), rendering the Wannier-Mott exciton model largely applicable.

(2) The absolute position of the free-particle bandgap renormalizes by an amount similar to the exciton binding energy in comparison to the respective $K - K$ transition in bulk. Thus, we observe only to a modest absolute shift of the exciton energy in optical spectra when comparing the bulk and monolayers.

(3) The Coulomb interaction deviates from the $1/r$ law due to the spatially inhomogeneous dielectric screening environment (see Sec. [II.B.2\)](#page-12-0). This changed distance dependence of the $e-h$ interaction strongly affects the energy spacing of the $n = 1, 2, 3...$ exciton states, leading to pronounced deviations from the 2D hydrogen model.

2. Effective Coulomb potential and the role of the environment

Calculations of excitonic states and binding energies in TMD MLs have been performed by many approaches, including effective mass methods, atomistic tight-binding and density functional theory approaches with various levels of sophistication, see, e.g., (Berghäuser [and Malic,](#page-24-28) [2014;](#page-24-28) [Cheiwchanchamnangij and Lambrecht,](#page-24-7) [2012;](#page-25-27) [Komsa and Krasheninnikov,](#page-25-27) 2012; Molina-Sánchez [et al.](#page-26-8), [2013;](#page-26-8) Qiu [et al.](#page-27-4), [2013;](#page-27-4) [Ramasubramaniam,](#page-27-5) [2012;](#page-27-5) Shi [et al.](#page-27-19), [2013a;](#page-27-19) [Stroucken and Koch,](#page-28-25) [2015;](#page-28-25) [Trushin](#page-28-26) [et al.](#page-28-26), [2016;](#page-28-26) Wu [et al.](#page-28-27), [2015a\)](#page-28-27). A simple and illustrative approach to calculate energies of exciton states is provided by the effective mass method. Here, in the Hamil-tonian [\(2\)](#page-9-1), the single-particle kinetic energies $\mathcal{H}_e(\mathbf{k}_e)$ and $\mathcal{H}_h(\boldsymbol{k}_h)$ are replaced by the operators $-\hbar^2/(2m_e)\partial^2/\partial \boldsymbol{\rho}_e^2$ and $-\hbar^2/(2m_h)\partial^2/\partial \rho_h^2$, respectively, with ρ_e , ρ_h being the electron and hole in-plane position vectors. Most importantly, the electric field between individual charges in the ML permeates both the material layer and the surroundings outside the monolayer. As a consequence, both the strength and the form of the effective Coulomb

Material	Sample (Temp.)	Exp. technique	Bind. energy [eV]	Bandgap [eV]	Reference
WSe ₂	Exf. on SiO_2/Si (RT)	Refl., 2P-PLE	0.37	2.02	He et al., 2014
	CVD on $HOPG$ (79 K)	STS, PL	$0.5\,$	2.2 ± 0.1	Zhang et al., 2015a
	Exf. on SiO_2/Si (4K)	PLE, 2P-PLE, SHG	0.6 ± 0.2	2.35 ± 0.2	Wang $et \ al., 2015a$
	Exf. on SiO_2/Si (4, 300 K)	Refl.	0.887	2.63	Hanbicki et al., 2015
	CVD on HOPG $(77 K)$	STS, PL	$\approx 0.4*$	2.08 ± 0.1	Chiu <i>et al.</i> , 2015
	Exf. on diamond ₂ (RT)	Mid-IR pump-probe	0.245	$1.9***$	Poellmann et al., 2015
WS_2	Exf. on SiO_2/Si (5K)	Refl.	0.32 ± 0.04	2.41 ± 0.04	Chernikov et al., 2014
	Exf. on fused silica $(10K)$	$2P-PLE$	0.7	2.7	Ye <i>et al.</i> , 2014
	Exf. on SiO_2/Si (RT)	$2P-PLE$	0.71 ± 0.01	2.73	Zhu et al., $2014a$
	Exf. on SiO_2/Si (4, 300 K)	Refl.	0.929	3.01	Hanbicki et al., 2015
	Exf. on fused silica (RT)	Refl., PLE	0.32 ± 0.05	2.33 ± 0.05	Hill <i>et al.</i> , 2015
	Exf. on fused silica (RT)	STS, Refl.	0.36 ± 0.06	2.38 ± 0.06	Rigosi <i>et al.</i> , 2016
	CVD on $SiO2$ (4K)	Magneto-refl.	$0.26 - 0.48$	$2.31 - 2.53$ ***	Stier <i>et al.</i> , 2016a
MoSe ₂	MBE on 2L graphene/SiC $(5K)$	STS, PL	0.55	2.18	Ugeda et al., 2014
	CVD on HOPG $(79K)$	STS, PL	0.5	2.15 ± 0.06	Zhang $et \ al.,\ 2015a$
MoS ₂	CVD on HOPG (77K)	STS, PL	0.2 (or 0.42)	2.15 ± 0.06	Zhang et al., 2014a
	Exf., suspended $(77 K)$	$_{\rm PC}$	>0.57	2.5	Klots <i>et al.</i> , 2014
	Exf. on hBN/fused silica (RT)	PLE	$0.44{\pm0.08}$ **	2.47 ± 0.08 **	Hill <i>et al.</i> , 2015
	CVD on HOPG (77K)	STS, PL	$\approx 0.3*$	2.15 ± 0.1	Chiu et al., 2015
	Exf. on fused silica (RT)	STS, Refl.	0.31 ± 0.04	2.17 ± 0.1	Rigosi et al., 2016

TABLE II Summary of experimentally determined exciton binding energies and free particle bandgaps in monolayer TMDs from the literature. All values correspond to the A-exciton transition, unless noted otherwise. The numerical formats correspond to the presentations of the data in the respective reports.

* extracted from the PL data and STS results in Ref. Chiu [et al.](#page-24-20), [2015](#page-24-20)

** attributed to the B-exciton transition by the authors of Ref. Hill *[et al.](#page-25-23)*, [2015](#page-25-23)

*** obtained by adding the estimated exciton binding energies to the resonance energy in Refs. [Poellmann](#page-27-18) et al., [2015;](#page-27-18) Stier [et al.](#page-28-24), [2016a](#page-28-24)

interaction between the electron and hole in the exciton are strongly modified by the dielectric properties of the environment (Raja [et al.](#page-27-13), [2017;](#page-27-13) Stier [et al.](#page-28-19), [2016b\)](#page-28-19). In principle, one recovers a 2D hydrogen-like problem with an adjusted effective potential by taking into account the geometry of the system and the dielectric surroundings [\(Berkelbach](#page-24-29) et al., [2013;](#page-24-29) [Chernikov](#page-24-8) et al., [2014;](#page-24-8) [Cu](#page-25-19)[dazzo](#page-25-19) et al., [2011;](#page-25-19) [Ganchev](#page-25-28) et al., [2015;](#page-25-28) [Keldysh,](#page-25-20) [1979;](#page-25-20) [Rytova,](#page-27-16) [1967\)](#page-27-16).

Typically, the combined system "vacuum + TMD monolayer $+$ substrate" is considered, reproducing the main features of the most common experimentally studied samples. In the effective medium approximation, the dielectric constant $\varepsilon \sim 10$ of the TMD ML generally far exceeds the dielectric constants of the surroundings, i.e., of the substrate ε_s and of the vacuum. As a result, the effective interaction potential takes the form of $\propto 1/\rho$ $(\rho = \rho_e - \rho_h)$ is the relative electron-hole coordinate) only at large distances between the particles where the electrical field resides outside the TMD ML itself. At smaller distances, the dependence is $\propto \log(\rho)$ [\(Cudazzo](#page-25-19) [et al.](#page-25-19), [2011\)](#page-25-19). The resulting overall form of the effective potential, following [\(Keldysh,](#page-25-20) [1979;](#page-25-20) [Rytova,](#page-27-16) [1967\)](#page-27-16), is approximated by

$$
V(\rho) = -\frac{\pi e^2}{(1+\varepsilon_s)r_0} \left[\mathbf{H}_0 \left(\frac{\rho}{r_0} \right) - Y_0 \left(\frac{\rho}{r_0} \right) \right],\qquad(3)
$$

where $\mathbf{H}_0(x)$ and $Y_0(x)$ are the Struve and Neumann functions, r_0 is the effective screening length. The latter can either be calculated from ab-intio [\(Berkelbach](#page-24-29) et al., [2013\)](#page-24-29) or considered as a phenomenological parameter of the theory [\(Chernikov](#page-24-8) et al., [2014\)](#page-24-8) and typically ranges from roughly 30 Å to 80 Å. Then, within the effective mass approximation, the two-particle Schrödinger equation with the effective potential $V(\rho)$ in the form of Eq. [\(3\)](#page-13-1) can be solved, e.g., variationally and numerically or, in some cases analytically [\(Ganchev](#page-25-28) et al., [2015\)](#page-25-28). The result is a series of exciton states described by the envelope functions of the relative motion $\varphi_{nm}(\rho)$. Overall, the model potential in the form [\(3\)](#page-13-1) describes the deviations from the ideal 2D hydrogenic series observed in the experiments and can be used as an input in more sophisticated calculations of excitonic spectra (Berghäuser and Malic, [2014;](#page-24-28) [Steinhoff](#page-27-20) *et al.*, [2014\)](#page-27-20). This simple model potential also agrees well with the predictions from high-level *ab-intio* calculations using Bethe-Salpeter equation approach [\(Chaves](#page-24-30) *et al.*, [2017;](#page-24-30) [Latini](#page-26-25) et al., [2015;](#page-26-25) Qiu [et al.](#page-27-4), [2013;](#page-27-4) [Ugeda](#page-28-20) et al.,

[2014;](#page-28-20) [Wang](#page-28-7) et al., [2015a;](#page-28-7) Ye [et al.](#page-28-22), [2014\)](#page-28-22).

Although a reasonably adequate description of the experimental data for the exciton binding energies is already provided by the relatively simple effective mass model with an effective potential in the form of Eq. [\(3\)](#page-13-1), there are several issues debated in the literature that require further studies:

• Since the exciton binding energy typically exceeds phonon energies both in TMD ML [\(Zhang](#page-29-17) et al., [2015c\)](#page-29-17) and in typical substrates, static screening is not necessarily well justified (Stier *[et al.](#page-28-19)*, [2016b\)](#page-28-19). However, the frequency range at which the screening constant should be evaluated and whether high-energy optical phonons play a role merits further investigation.

• Depending on the material and the substrate, the binding energy can be as large as $1/4 \dots 1/3$ of the band gap, see Tab. [II.](#page-13-0) The excitons have also a relatively small radii leading to a sizable extension of the wavefunction in reciprocal space. Therefore, the effective mass model may not always provide quantitatively accurate results and the effects of the band non-parabolicity and the spin-orbit coupling should be included.

• In addition, the trigonal symmetry of the TMD MLs results in the mixing of the excitonic states (n, m) with different m particularly, in the mixing of the s- and p-shell excitons (i.e., the states with $m = 0$ and $|m| = 1$) as demonstrated theoretically in Ref. [\(Glazov](#page-25-25) et al., [2017;](#page-25-25) Gong [et al.](#page-25-26), [2017\)](#page-25-26). Further studies of exciton mixing within ab-initio and tight-binding models to determine quantitatively the strength of this effect are required, in addition to more detailed one and two-photon excitation experiments.

• Also the ordering of 2s and 2p resonances remains an open issue in light of recent theoretical predictions of the state-mixing and the experimental challenges are to precisely determine the $2s/2p$ splitting in TMD MLs, i.e., by comparing the linear and nonlinear absorption spectra or by detailed studies of magneto-optical properties in high-quality MLs, and the eventual splitting of the 2p states [\(Srivastava and Imamoglu,](#page-27-17) [2015;](#page-27-17) Wu [et al.](#page-28-27), [2015a;](#page-28-27) Zhou [et al.](#page-29-18), [2015\)](#page-29-18).

• On the experimental side, controlling the influence of the dielectric screening of the surroundings is of particular importance. Recent works on this topic include observations of exciton states in different solutions [\(Lin](#page-26-26) [et al.](#page-26-26), [2014;](#page-26-26) Ye [et al.](#page-28-22), [2014\)](#page-28-22), measurements of changes in the exciton Bohr radii from diamagnetic shifts on different substrates (Stier [et al.](#page-28-19), [2016b\)](#page-28-19) and demonstration of the bandgap and exciton energy renormalization due to external dielectric screening [\(Raja](#page-27-13) et al., [2017\)](#page-27-13).

• Further questions arise with respect to the uniformity of the dielectric environment, with possible variations of the sample-substrate distance and the non-uniform coverage by adsorbates, also considering the recently predicted nanometer spatial sensitivity of the screening effect (Rösner *et al.*, [2016\)](#page-27-21). Here experimental comparisons between different capped and uncapped samples will be helpful as well to study, for example, the influence of the substrate morphology on the exciton states.

C. Light-matter coupling via excitons

1. Dark and bright excitons

When generated by resonant photon absorption under normal incidence, excitons are optically *bright* (see also discussion in Sec. [II.C.3\)](#page-17-0). Subsequent scattering events with other excitons, electrons, or phonons, and defects can induce spin flips and considerable changes in exciton momentum. Alternatively, in case of a more complex generation process such as non-resonant optical excitation or electrical injection, a variety of exciton states can form. As a result of all the above, an exciton may not necessarily be able to recombine radiatively, for instance if the optical transition is now spin forbidden. Such an exciton is described as optically dark. Another way to generate dark excitons is if a hole and an electron, for instance injected electrically, come together to form an exciton with total angular momentum $\neq 1$ or large centerof-mass momentum K_{exc} . So whether or not excitons can directly interact with light either through the absorption or emission of a single photon, depends on the center of mass wavevector K_{exc} , the relative motion wavefunction, the valley, τ_e (τ_h), and spin, s_e (s_h), states of the electron and hole.

In TMD MLs, exciton-photon coupling is governed by chiral optical selection rules: For normally incident light the direct interband transitions at the K^{\pm} points of the Brillouin zone are active for σ^{\pm} light polarization, Fig. [1c](#page-5-1),d (Cao [et al.](#page-24-6), [2012;](#page-24-6) Mak [et al.](#page-26-16), [2012;](#page-26-16) [Sallen](#page-27-8) [et al.](#page-27-8), [2012;](#page-27-8) Xiao [et al.](#page-28-6), [2012;](#page-28-6) Yao [et al.](#page-28-12), [2008;](#page-28-12) [Zeng](#page-29-9) [et al.](#page-29-9), [2012\)](#page-29-9). Considering interband transitions, the spin and valley states of the electron are conserved and the electron and hole are generated within the same unit cell. As a result, the ns-shell excitonic states (i.e., those with $m = 0$, such as $1s, 2s, 3s$, etc.) where the envelope function $\varphi_{ns}(0) \neq 0$, with $\tau_e = -\tau_h = +1$, $s_e = -s_h = +1/2$ are active in σ^+ polarization and the states with $\tau_e = -\tau_h = -1$, $s_e = -s_h = -1/2$ are active in σ^- polarization. The exciton states with $\tau_e = \tau_h$ (occupied electron states in CB and unoccupied electron states in VB) or $s_e = s_h$ (electron and unoccupied state have opposite spins) are dark [\(Glazov](#page-25-13) *et al.*, [2015\)](#page-25-13). A schematic illustration of bright and dark electron transitions corresponding to the respective exciton states is presented in Fig. [5a](#page-15-0). While the above rules describe the A-exciton series, they are essentially the same for the B-exciton states when the opposite signs of the corresponding spin indices are considered. Also, an admixing of the p-character to the s-like states is theoretically pre-dicted due to the exchange interaction [\(Glazov](#page-25-25) *et al.*, [2017;](#page-25-25) [Gong](#page-25-26) et al., [2017\)](#page-25-26) and disorder [\(Berghauser](#page-24-26) et al., [2017\)](#page-24-26) giving rise to modification of selection rules of oneor two-photon transitions.

 $\frac{1}{2}$ involving the spin states in the conduction band 1 and 2. For conduction band is for $\frac{1}{2}$ conduction band 1 and 2. For conduction band is to conduction band is to simplicity we do not show the Coulomb exchange energy term that also contributes to the dark-bright splitting [\(Echeverry](#page-25-7) K^{\pm} and Γ -O excitons *[et al.](#page-25-7)*, [2016\)](#page-25-7). (c) and (d) Using in-plane optical excitation and K^{\pm} and 1-Q excitons detection, the dark (X^D) and bright (X^0) exciton can be dispersed by particular points in the tinguished by polarization dependent measurements, adapted from (Wang *et al.*, [2017\)](#page-28-16). The WSe₂ ML is encapsulated in (a) hBN for improved optical quality. **BEN EXP** to have a spin state of K^+ FIG. 4 (a) Brightening of the dark exciton transition spin configuration are observed in ML WSe₂ by photoluminescence experiments Of similar with in an in-plane magnetic field [\(Zhang](#page-29-7) et al., [2017\)](#page-29-7) (b) excitons are Schematic of the brightening of the dark exciton transitions the direct transitions simplicity we do not show the Coulomb exchange energy term servation. E

for neutral 1s excitons, the order and energy dirperpendicular to the ML plane, Fig. 1(a,b). Attocube For neutral 1s excitons, the order and energy difference between bright and dark excitons is given by the sign and amplitude of the spin splitting in the conduction band and the short-range Coulomb exchange interaction, Dark Dark similar to the situation in quantum dots (Crooker et al., [2003\)](#page-25-29). For WS_2 and WSe_2 , the *electron* spin orientations $\frac{2000}{100}$. The last $100₂$ and $100₂$, in a constraint power conductions, in the upper valence band and in the lower conduction $\frac{1}{2}$ hand are opposite while in M_0S_2 and M_0S_3 , the spins are parallel, as shown in Fig. [1c](#page-5-1),d, although recent studies discuss the possibility of the ground state in ML MoX₂ FIG. 5 (a) the same of the samples of the sample of the same of the ratio $\frac{1}{2}$ forbidden electric being dark [\(Baranowski](#page-24-11) *et al.*, [2017;](#page-24-11) [Molas](#page-26-15) *et al.*, [2017\)](#page-26-15). t_{out} the focus spot diameter spot diameter spot diameter and the thickness band are opposite, while in $MoS₂$ and $Mose₂$, the spins

As a result, the lowest lying CB to VB transition is $\frac{a}{\text{fed}}$ for clarity spin forbidden (dark) in WS_2 and WSe_2 , the spin allowed and the high-transition is at higher energy as indicated in Fig. [4.](#page-15-1) One band. The or $\frac{1}{\sqrt{2}}$ experimental approach to measure the energy splitting corresponds to $\frac{1}{2}$ interaction of the longer interaction of the longer interaction of the K-valley strong inbetween the dark and bright state is to apply a strong in $\frac{201}{3}$, refinant
plane magnetic field. This leads to an admixture of bright. (b) Schematic and dark states which allows detection the dark transi-
bright oxidence bright on the two spin-orbit splitting is print to the spin-orbit space of the spin-orbit space of the spin-orbit space of the spin-orbit space of the plane magnetic field. This leads to an admixture of bright (b) Schematic tions that gain oscillator strength and appear in the spectrum as the magnetic field increases, see Fig. [4a](#page-15-1),b [\(Molas](#page-26-15) [et al.](#page-26-15), [2017;](#page-26-15) [Zhang](#page-29-7) et al., [2017\)](#page-29-7). For ML WSe₂, the dark excitons lie about 40 meV below the bright transitions.

tically allowed with a dipole out of the monolayer plane In addition to spin conservation, there is another important differences between the so called bright and dark excitons: Symmetry analysis [\(Glazov](#page-25-12) et al., [2014;](#page-25-12) [Slobo](#page-27-22)[deniuk and Basko,](#page-27-22) [2016a;](#page-27-22) [Wang](#page-28-11) et al., [2017;](#page-28-11) [Zhou](#page-29-8) et al., [2017\)](#page-29-8) shows that the spin-forbidden dark excitons are op-(z-mode), whereas the spin-allowed bright excitons have their dipole in the monolayer plane xy . Therefore optical excitation and detection in the plane of the monolayer (i.e., in the limit of grazing incidence) allows a more efficient detection of these in principle spin-forbidden transitions than experiments with excitation/detection normal to the monolayer, as indicated in Fig. [4c](#page-15-1),d. This allowed exciton, lies in mixing of bands with different spin configuration and orbital origin.

Of similar origin as the spin-forbidden intra-valley dark excitons are the spin-allowed inter-valley states, where the direct transition of the electron from the valence to conduction band is forbidden due to the momentum conservation. Examples are inter-valley K^{\pm} - K^{\mp} , K^{\pm} - Q , Γ- K^{\pm} and Γ -Q excitons, where K^{\pm} , Q and Γ refer to the particular points in the Brillouin zone.

FIG. 5 (a) A schematic overview of typical allowed and forbidden electronic transitions for the respective bright and dark exciton states. The underlying band structure is simplified for clarity, including only the upper valence band at K^+ and the high-symmetry points K^{\pm} and Q in the conduction band. The order of the spin states in the conduction band, corresponds to W-based TMD MLs, see Refs. [\(Glazov](#page-25-12) et al., [2014;](#page-25-12) [Kormanyos](#page-25-4) et al., [2015;](#page-25-4) Liu [et al.](#page-26-14), [2013\)](#page-26-14) for details. (b) Schematic illustration of the exciton ground-state dispersion in the two-particle representation. The light-cone for bright excitons is marked by the free-space photon-dispersion, cq_{\parallel} , where c is the speed of light and the excitons outside of the cone are essentially dark.

2. Radiative lifetime

An additional constraint on the optical activity of the excitons is imposed by the center-of-mass wavevector conservation K_{exc} , which should be equal to the projection of the photon wavevector q_{\parallel} on the TMD ML plane. The range of the wavevectors meeting this requirement obeys, for a ML in vacuum, the condition $K_{\rm exc} \leqslant q_0 = \omega_0/c$, where ω_0 is the photon frequency corresponding to the exciton resonance (for 1s exciton $\omega_0 = (E_g - E_B)/\hbar$. Bright excitons within this socalled "light cone" couple directly to light, i.e., can be either be created by the absorption of a photon or spontaneously decay through photon emission, while excitons with $K_{\text{exc}} > q_0$ are optically inactive.

In general, the radiative decay rate Γ_0 of the bright excitons within the light cone, which also determines the overall strength of optical absorption (i.e., total area of the resonance), is proportional to the probability of finding the electron and the hole within the same unit cell, i.e., to $|\varphi_{ns}(0)|^2 \propto 1/a_B^2$, where a_B is the effective Bohr radius. The strong Coulomb interaction in TMD MLs, leading to the large binding energies of the excitons, also results in relatively small exciton Bohr radii, $a_B \sim 1$ nm for the 1s state, as discussed above. Estimates of Γ_0 for the 1s exciton within a simple two-band model [\(Glazov](#page-25-12) [et al.](#page-25-12), [2014,](#page-25-12) [2015\)](#page-25-13) then yield $\hbar\Gamma_0 \gtrsim 1$ meV. This corresponds to a radiative decay time $1/(2\Gamma_0) \lesssim 1$ ps, in good agreement with experimental observations [\(Jakubczyk](#page-25-30) [et al.](#page-25-30), [2016;](#page-25-30) [Moody](#page-26-27) et al., [2015;](#page-26-27) [Palummo](#page-26-28) et al., [2015;](#page-26-28) [Poellmann](#page-27-18) et al., [2015;](#page-27-18) [Robert](#page-27-23) et al., [2016\)](#page-27-23). Hence, the radiative decay times of excitons in TMD MLs are about two orders of magnitude shorter as compared, e.g., with the excitons in GaAs-based quantum wells [\(Deveaud](#page-25-31) [et al.](#page-25-31), [1991\)](#page-25-31). In addition, the radiative broadening on the order of 1 meV imposes a lower limit on the total linewidth of the bright exciton resonance [\(Cadiz](#page-24-15) et al., [2017;](#page-24-15) Dey [et al.](#page-25-32), [2016;](#page-25-32) [Jakubczyk](#page-25-30) et al., [2016;](#page-25-30) [Moody](#page-26-27) [et al.](#page-26-27), [2015\)](#page-26-27). This simple analysis is further corroborated by first principle calculations, which predict exciton intrinsic lifetimes as short as hundreds of fs [\(Palummo](#page-26-28) [et al.](#page-26-28), [2015;](#page-26-28) [Wang](#page-28-28) et al., [2016b\)](#page-28-28).

Importantly, the presence of the radiative cone determines the overall effective decay rate of an exciton population at finite temperatures through the radiative recombination channel. Which fraction of excitons is within and which fraction is outside the light cone depends on temperature [\(Andreani](#page-24-31) et al., [1991\)](#page-24-31). The effective radiative decay for thermalized populations is obtained from the radiative decay rate within the light cone Γ_0 , weighted by the fraction of the excitons inside the cone. In case of strictly 2D systems with a parabolic exciton dispersion, above very low temperatures, this fraction decreases linearly with the temperature [\(Andreani](#page-24-31) et al., 1991). For $MoS₂$, the effective radiative recombination time is calculated to be on the order of several tens of ps at cryogenic temperatures and to exceed a nanosecond at room temperature [\(Wang](#page-28-28) et al., [2016b\)](#page-28-28). While radiative recombination is forbidden outside the light cone if wavevector conservation holds, this can be partially relaxed due to the presence of disorder caused, e.g., by impurities or defects, since momentum conservation is relaxed in disordered systems [\(Citrin,](#page-25-33) [1993;](#page-25-33) [Vinattieri](#page-28-8) [et al.](#page-28-8), [1994\)](#page-28-8).

The effective radiative lifetime is, of course, also affected by the presence of the spin-forbidden intra-valley and inter-valley dark states considering thermal distribution of excitons between these states. It further depends on the relaxation rate of the dark excitons of the reservoir towards low-momentum states [\(Slobode](#page-27-24)[niuk and Basko,](#page-27-24) [2016b\)](#page-27-24), potentially leading to the additional depletion of the excitons within the radiative cone [\(Kira and Koch,](#page-25-34) [2005\)](#page-25-34). When the excitons are predominantly created within the radiative cone through resonant or near-resonant excitation, an initial ultra-fast decay has been indeed observed [\(Poellmann](#page-27-18) et al., [2015;](#page-27-18) [Robert](#page-27-23) et al., [2016\)](#page-27-23) and attributed to the intrinsic radiative recombination time Γ_0 of the bright states. The excitons were shown to thermalize subsequently and to experience slower decay at later times. At room temperature, effective radiative exciton lifetimes as long as 20 ns have been measured in super-acid treated samples [\(Amani](#page-24-32) et al., [2015\)](#page-24-32) and estimated to be on the order of 100 ns from combined time-resolved PL and quantum yield measurements (Jin [et al.](#page-25-35), [2017\)](#page-25-35).

Finally we note, that the overall decay of the exciton population is usually governed by the complex interplay of radiative and non-radiative channels. It is thus affected by the presence of defects and disorder, Auger-type exciton-exciton annihilation at elevated densities [\(Kumar](#page-26-29) [et al.](#page-26-29), [2014a;](#page-26-29) [Mouri](#page-26-30) et al., [2014;](#page-26-30) Sun [et al.](#page-28-29), [2014;](#page-28-29) Yu [et al.](#page-29-19), [2016\)](#page-29-19), and through the formation of exciton complexes such as biexcitons (Sie [et al.](#page-27-25), [2015a;](#page-27-25) You [et al.](#page-28-30), [2015\)](#page-28-30) and trions (Mak [et al.](#page-26-31), [2013;](#page-26-31) Ross [et al.](#page-27-26), [2013\)](#page-27-26). Finally, radiative recombination itself depends on the optical environment, i.e., the effective density of the photon modes available as final states for the recombination of the excitons. The effective strength of the light-matter interaction is thus modified by the optical properties of the surroundings (e.g., refractive index of the substrate) and can be tuned externally. The integration of the TMD MLs in optical cavities highlights this aspect. Indeed, the strongcoupling regime has been demonstrated, where excitons and photons mix to create hybrid quasiparticles, exciton polaritons [\(Dufferwiel](#page-25-36) et al., [2015;](#page-25-36) [Flatten](#page-25-37) et al., [2016;](#page-25-37) Liu [et al.](#page-26-32), [2015b;](#page-26-32) [Lundt](#page-26-33) et al., [2016;](#page-26-33) [Sidler](#page-27-27) et al., [2016;](#page-27-27) [Vasilevskiy](#page-28-31) et al., [2015\)](#page-28-31). The discussion above highlights the complex challenges for interpreting for example photoluminescence emission times measured in experiments in terms of intrinsic decay rates, effective radiative lifetimes and non-radiative channels, for example.

In many spectroscopy experiments performed on TMDs monolayers involving optical injection, the excitation laser energy is larger than the exciton ground state energy. This means that exciton formation dynamics and energy relaxation have to be taken into account. Two exciton formation processes are usually considered in semiconductors: (i) direct hot exciton photogeneration, with the simultaneous emission of phonons, in which the constitutive electron-hole pair is geminate [\(Bonnot](#page-24-33) [et al.](#page-24-33), [1974\)](#page-24-33); or (ii) bimolecular exciton formation which consists of direct binding of electrons and holes [\(Barrau](#page-24-34) [et al.](#page-24-34), [1973;](#page-24-34) [Piermarocchi](#page-27-28) et al., [1997\)](#page-27-28). In 2D semiconductors based on GaAs quantum wells the bimolecular formation process plays an important role [\(Amand](#page-24-35) et al., [1994;](#page-24-35) [Piermarocchi](#page-27-28) et al., [1997;](#page-27-28) [Szczytko](#page-28-32) et al., [2004\)](#page-28-32). When the excitation energy lies below the free particle bandgap in TMD monolayers, the exciton formation process can only be geminate (neglecting Auger like and two-photon absorption effects). Note that this process, which involves a simultaneous emission of phonons, can yield the formation of either intra-valley or inter-valley excitons. When the excitation energy is strongly nonresonant, i.e. above the free particle bandgap, the PL dynamics is very similar compared to the quasi-resonant excitation conditions in $MoS₂$ or $WSe₂$ monolayers [\(Korn](#page-26-22) [et al.](#page-26-22), [2011;](#page-26-22) [Wang](#page-28-33) et al., [2014;](#page-28-33) [Zhang](#page-29-6) et al., [2015d\)](#page-29-6). The PL rise time is still very short and no signature of bimolecular formation and energy relaxation of hot excitons can be evidenced, in contrast to III-V or II-VI quantum wells. Indeed, recent reports indicate ultra-fast exciton formation on sub-ps timescales after non-resonant excitation [\(Ceballos](#page-24-36) et al., [2016;](#page-24-36) Cha [et al.](#page-24-27), [2016;](#page-24-27) [Stein](#page-28-34)[leitner](#page-28-34) *et al.*, [2017\)](#page-28-34). While further studies are required, at this stage one can already speculate that the strongexciton phonon coupling in TMD monolayers seems to yield efficient exciton formation process for a wide range of excitation conditions. We also note, that alternative processes such as multi-exciton generation, i.e., the reverse of Auger-type annihilation, might become important for sufficiently high excess energies.

III. EXCITONS AT FINITE CARRIER DENSITIES

The discussion in the previous Section [II](#page-7-0) deals with the fundamental properties of the excitons in TMD MLs in the low-density regime. However, the presence of photoexcited carriers, either in the form of Coulomb-bound or free charges, can significantly affect the properties of the excitonic states, as is the case for traditional 2D systems with translational symmetry, such as quantum wells [\(Haug and Koch,](#page-25-14) [2009\)](#page-25-14).

A. The intermediate and high density regimes

We distinguish two partially overlapping regimes of *in*termediate and high density conditions. These can be defined as follows: In the intermediate density regime the excitons can still be considered as bound electron-hole pairs, but with properties considerably modified compared with the low-density limit. In the high density regime, beyond the so-called Mott transition, excitons are no longer bound states; the electrons and holes are more appropriately described as a dense Coulomb-correlated gas. Under such conditions, the conductivity of the photoexcited material behaves less like the insulating semiconductor with neutral excitons and more like a metal with many free carriers, whence the description of this effect as a photoinduced Mott transition. The transition between two regimes is controlled by the ratio of the average carrier-carrier (or, alternatively, exciton-exciton) separation $2/\sqrt{n\pi}$ to the exciton Bohr radius a_B at low density: For $2/(\sqrt{n\pi}a_B) \lesssim 1$ the density of carriers (or excitons) n can be considered as high. Due to the small Bohr radius of about 1 nm in TMD MLs, the intermediate and high density regimes are reached at significantly higher carrier densities compared to systems with weaker Coulomb interactions, such as III-V or II-VI semiconductor quantum wells. With respect to absolute numbers, the intermediate case with inter-particle distances about 100 to $10 \times a_B$, broadly covers the density range between 10^{10} and several 10^{12} cm⁻². The high density case then corresponds to separations on the order of a few Bohr radii or less and is considered to apply for carrier densities of a few 10^{13} to 10^{14} cm⁻² or higher. In particular, the electron-hole pair-density of $n = a_B^{-2}$, often used as a rough upper estimate for the Mott transition [\(Klingshirn,](#page-25-18) 2007), yields $n \sim 10^{14} \,\mathrm{cm}^{-2}$ for TMD MLs.

The main phenomena occurring at elevated carrier densities can be briefly summarized as follows:

• First, there are efficient scattering events. Elastic and inelastic scattering of excitons with free carriers or excitons leads to relaxation of the exciton phase, energy, momentum and spin and thus to spectral broadening of the exciton resonances [\(Chernikov](#page-24-37) et al., [2015b;](#page-24-37) [Dey](#page-25-32) [et al.](#page-25-32), [2016;](#page-25-32) [Moody](#page-26-27) et al., [2015;](#page-26-27) Shi [et al.](#page-27-29), [2013b;](#page-27-29) [Wang](#page-28-35) [et al.](#page-28-35), [1993\)](#page-28-35). In addition, through inelastic scattering with free charge carriers, an exciton can capture an additional charge and form a bound three-particle state at intermediate densities, the so-called trion states [\(Kheng](#page-25-38) [et al.](#page-25-38), [1993;](#page-25-38) Mak [et al.](#page-26-31), [2013;](#page-26-31) Ross [et al.](#page-27-26), [2013;](#page-27-26) [Singh](#page-27-30) $et \ al.,\ 2016a; Stébé and Ainane, 1989). Similarly, at in et \ al.,\ 2016a; Stébé and Ainane, 1989). Similarly, at in et \ al.,\ 2016a; Stébé and Ainane, 1989). Similarly, at in et \ al.,\ 2016a; Stébé and Ainane, 1989). Similarly, at in et \ al.,\ 2016a; Stébé and Ainane, 1989). Similarly, at in$ termediate exciton densities, interactions between excitons can result in a bound two-exciton state, the biexciton state [\(Miller](#page-26-34) et al., [1982;](#page-26-34) [Plechinger](#page-27-32) et al., [2015;](#page-27-32) [Shang](#page-27-33) [et al.](#page-27-33), [2015;](#page-27-33) Sie [et al.](#page-27-25), [2015a;](#page-27-25) You [et al.](#page-28-30), [2015\)](#page-28-30), resembling the hydrogen molecule.

Charged excitons (trions) and biexcitons were predicted for bulk semiconductors [\(Lampert,](#page-26-35) [1958\)](#page-26-35) by analogy with molecules and ions. While they naturally appear as a result of Coulomb interactions between three or four charge carriers, we also note that in real systems with finite carrier densities, the correlations between, e.g., excitons/trions and the Fermi sea of electrons (or holes) may be of importance [\(Efimkin and Mac-](#page-25-39)[Donald,](#page-25-39) [2017;](#page-25-39) [Sidler](#page-27-27) et al., [2016;](#page-27-27) [Suris,](#page-28-36) [2003\)](#page-28-36). Furthermore, excitons formed from two fermions can be considered as composite bosons at least for not too high carrier densities. Interestingly, excitons are expected to demonstrate at low to intermediate densities collective phenomena such as Bose-Einstein condensation (strictly speaking, quasi-condensation in two-dimensions) and superfluidity [\(Fogler](#page-25-40) et al., [2014;](#page-25-40) [Keldysh and Kozlov,](#page-25-41) [1968;](#page-25-41) [Moskalenko,](#page-26-36) [1962\)](#page-26-36). First signatures of boson scattering of excitons in monolayer $WSe₂$ have been reported [\(Manca](#page-26-21) et al., [2017\)](#page-26-21). Additionally, exciton-exciton scattering can also lead to an Auger-like process: the nonradiative recombination of one exciton and dissociation of the other into an unbound electron and hole, leading to exciton-exciton annihilation, as already mentioned in Sec. [II.C.2](#page-16-0) [\(Kumar](#page-26-29) et al., [2014a;](#page-26-29) [Mouri](#page-26-30) et al., [2014;](#page-26-30) [Robert](#page-27-23) et al., [2016;](#page-27-23) Sun [et al.](#page-28-29), [2014;](#page-28-29) Yu [et al.](#page-29-19), [2016\)](#page-29-19).

• Second, finite quasiparticle densities generally lead to what can be broadly called dynamic screening of the Coulomb interaction [\(Haug and Koch,](#page-25-14) [2009;](#page-25-14) [Klingshirn,](#page-25-18) [2007\)](#page-25-18). In analogy to the behavior of quasi-free carriers in metals, it is related to both direct and exchange contributions and typically decreases the effective strength of the Coulomb interaction. As a result of the decreasing electron-hole attraction, the exciton binding energy is reduced; the average electron-hole separation increases, thus also leading to lower oscillator strengths for excitonic transitons i.e. a to weaker light-matter coupling. In addition, the photoinduced screening induces renormalization of the free particle band gap to lower energies. In many cases, including TMD MLs, the decrease of the exciton ground-state $(n = 1)$ binding energy and the red shift of the bandgap are of similar magnitude, at least in the intermediate-density regime. Hence, while the absolute shifts of the $n = 1$ resonance, i.e., of the optical band gap (see Fig. [2\)](#page-6-0), can be rather small, on the order of several tens of meV, the underlying changes in the nature of excitations (binding energies, free-particle band gap) are about an order of magnitude larger [\(Chernikov](#page-24-38) et al., [2015a,](#page-24-38)[b;](#page-24-37) [Steinhoff](#page-27-20) et al., [2014;](#page-27-20) [Ulstrup](#page-28-37) et al., [2016\)](#page-28-37).

• Third, the presence of free carriers decreases the available phase space for the electron-hole complexes due to the Pauli blocking [\(Haug and Koch,](#page-25-14) [2009\)](#page-25-14). This also results in a decrease of trion and exciton binding energies and the oscillator strengths. In addition, at sufficiently high densities of both electrons and holes, it results in population inversion, i.e., more electrons populating the conduction rather than valence band over a certain range of energy. As in quantum wells [\(Haug and Koch,](#page-25-14) [2009\)](#page-25-14), this regime is expected to roughly coincide with the Mott transition discussed above. Moreover, in the high-density regime, bound electron-hole states cannot be formed and thus the optical spectra are no longer dominated by the exciton resonance. Population inversion then leads

to stimulated emission processes and negative absorp-tion for the corresponding transitions [\(Chernikov](#page-24-38) et al., [2015a;](#page-24-38) [Haug and Koch,](#page-25-14) [2009\)](#page-25-14). In the absence of competing scattering and absorption channels in the respective energy range, this would give rise to amplification of radiation and allow in principle for the use of the material as an active medium in lasing applications; see Refs. [\(Sale](#page-27-34)[hzadeh](#page-27-34) et al., [2015;](#page-27-34) Wu [et al.](#page-28-38), [2015b;](#page-28-38) Ye [et al.](#page-28-39), [2015\)](#page-28-39) for reports of lasing in TMD MLs.

Many issues in the high-density regime still remains to be explored, both experimentally and theoretically, the prepondence of literature on TMD monolayers having addressed the behavior of the materials at intermediate densities (Korn [et al.](#page-26-22), [2011;](#page-26-22) [Kumar](#page-26-37) et al., [2014b;](#page-26-37) [Lagarde](#page-26-38) et al., [2014;](#page-26-38) Mai [et al.](#page-26-39), [2014a;](#page-26-39) [Poellmann](#page-27-18) et al., [2015;](#page-27-18) [Schmidt](#page-27-35) et al., [2016b;](#page-27-35) [Singh](#page-27-36) et al., [2014;](#page-27-36) [Wang](#page-28-40) [et al.](#page-28-40), [2013;](#page-28-40) Zhu [et al.](#page-29-20), [2014b\)](#page-29-20). We also note that an accurate, quantitative treatment of many-body physics of strongly interacting systems is a very challenging problem. Promising steps in that direction are presented, for example in [\(Schmidt](#page-27-35) et al., [2016b;](#page-27-35) Selig [et al.](#page-27-37), [2016;](#page-27-37) [Steinhoff](#page-27-38) et al., [2015,](#page-27-38) [2014\)](#page-27-20). Although effects related with occupation of other $(Q \text{ and } \Gamma)$ valleys with an increase in the free-carrier density are of interest, the relative simplicity of the electronic structure of TMD monolayers, their tunability under external conditions and dielectric media, and experimental accessibility and their strong many-body effects make these systems promising test cases for advancing our understanding of fundamental issues in many-body interactions at high densities.

B. Electric charge control

While neutral excitons tend to dominate the optical properties of ML TMDs, more complex exciton species also play an important role. Particularly prevalent are charged excitons or trions, the species formed when an exciton can bind another electron (or hole) to form a negatively (or positively) charged three-particle state. Since unintentional doping in TMD layers is often n-type [\(Ayari](#page-24-39) et al., [2007;](#page-24-39) [Radisavljevic](#page-27-12) et al., [2011a\)](#page-27-12), the formation of negative trions is likely, assuming that adsorbates do not introduce additional significant changes to the doping level. In general, the trion binding energy in semiconductor nano-structures is typically 10% of the exciton binding energy [\(Van der Donck](#page-25-42) et al., [2017\)](#page-25-42). For a neutral exciton binding energy on the order of 500 meV, this yields an estimated trion binding energy of several tens of meV.

In monolayer $MoS₂$, Mak and coworkers observed tightly bound negative trions with a binding energy of about 20 meV (Mak *[et al.](#page-26-31)*, [2013\)](#page-26-31), see Fig. [6a](#page-19-2), which is one order of magnitude larger than the binding energy in well-studied quasi-2D systems such as II-VI quantum wells [\(Kheng](#page-25-38) *et al.*, [1993\)](#page-25-38), where trions were first observed. At low temperature in monolayer $MoSe₂$, well-separated neutral and charged excitons are observed

FIG. 6 (a) Absorbance and photoluminescence experiments exhibiting signatures of neutral (A) and charged (A^{-}) excitons in a charge tunable MoS_2 monolayer (Mak *[et al.](#page-26-31)*, [2013\)](#page-26-31). (b) Color contour plot of PL from an electrically gated \mathbf{MoSe}_{2} monolayer that can be tuned to show emission from positively charged (X^+) to negatively charged (X^-) trion species [\(Ross](#page-27-3) [et al.](#page-27-3), [2014\)](#page-27-3). (c) Contour plot of the first derivative of the differential reflectivity in a charge tunable \mathbf{WSe}_2 monolayer. The n- and p-type regimes are manifested by the presence of X ⁺ and X[−] transitions. Around charge neutrality, the neutral exciton X^0 and an excited state X^{0*} are visible [\(Courtade](#page-25-43) [et al.](#page-25-43), [2017\)](#page-25-43).

with a trion binding energy of approximately 30 meV, as clearly demonstrated in charge tunable structures (Ross [et al.](#page-27-26), [2013\)](#page-27-26), see Fig. [6b](#page-19-2). In this work, the authors also show the full bipolar transition from the neutral exciton to either positively or negatively charged trions, depending on the sign of the applied gate voltage. The binding energies of these two kinds of trion species were

found to be similar, an observation consistent with only minor differences in the effective masses of electrons and holes in most of the studied TMDs [\(Kormanyos](#page-25-4) [et al.](#page-25-4), [2015;](#page-25-4) Liu [et al.](#page-26-14), [2013\)](#page-26-14). We also note, that in optical spectra, the energy separation between neutral excitons and trions is a sum of the trion binding energy (strictly defined for the zero-density case) and a term proportional to the Fermi energy of the free charge carriers, see, e.g., [\(Chernikov](#page-24-37) et al., [2015b;](#page-24-37) Mak [et al.](#page-26-31), [2013\)](#page-26-31). In addition to the trion signatures in PL and at sufficiently large free carrier densities, the signatures of the trions are also found in absorption-type measurements [\(Chernikov](#page-24-8) et al., [2014,](#page-24-8) [2015b;](#page-24-37) [Jones](#page-25-44) et al., [2013;](#page-25-44) Mak [et al.](#page-26-31), [2013;](#page-26-31) [Singh](#page-27-39) et al., [2016b\)](#page-27-39).

Electrical charge tuning of excitons is commonly observed in monolayer TMDs devices, also including $WSe₂$ [\(Jones](#page-25-44) *et al.*, [2013\)](#page-25-44) and $WS₂$ [\(Plechinger](#page-27-32) *et al.*, [2015;](#page-27-32) [Shang](#page-27-33) *et al.*, [2015\)](#page-27-33). In WS_2 , these two works also reported biexcitons in addition to neutral and charged excitons.

As a fundamental difference to conventional quantum well structures, in monolayer TMDs the carriers have an additional degree of freedom: the valley index. This leads to several optically bright and also dark configurations, for a classification, see e.g. [\(Courtade](#page-25-43) [et al.](#page-25-43), [2017;](#page-25-43) [Dery and Song,](#page-25-6) [2015;](#page-25-6) [Ganchev](#page-25-28) et al., [2015;](#page-25-28) Yu [et al.](#page-29-21), [2015b\)](#page-29-21), which can give rise to potentially complex recombination and polarization dynamics [\(Volmer](#page-28-41) et al., [2017\)](#page-28-41). Charge tunable monolayers that are encapsulated hexagonal boron nitride, result in narrow optical transitions, with low-temperature linewidths typically below 5 meV, as shown in Fig. [6c](#page-19-2). This has revealed the trion fine structure related to the occupation of the same or different valleys by the two electrons [\(Courtade](#page-25-43) et al., [2017;](#page-25-43) [Jones](#page-25-44) et al., [2013,](#page-25-44) [2016;](#page-25-45) [Plechinger](#page-27-40) et al., [2016;](#page-27-40) [Singh](#page-27-39) et al., [2016b\)](#page-27-39). An informative comparison between charge tuning in ML $WSe₂$ and ML MoSe₂ was recently reported in [Wang](#page-28-16) [et al.](#page-28-16) [\(2017\)](#page-28-16) and revealed the highest-energy valence band and the lowest-energy conduction band to have antiparallel spins in ML WSe2, and parallel spins in ML MoSe2. The concept of the trion as a three particle complex is useful at low carrier densities; at elevated densities intriguing new many-body effects have been predicted by several groups [\(Dery,](#page-25-46) [2016;](#page-25-46) [Efimkin and](#page-25-39) [MacDonald,](#page-25-39) [2017;](#page-25-39) [Sidler](#page-27-27) *et al.*, [2016\)](#page-27-27).

IV. VALLEY POLARIZATION DYNAMICS

A. Valley-polarized excitons

Optical control of valley polarization is one of the most fascinating properties of TMD monolayers. In the majority of cases, due to the strong Coulomb interaction, the valley dynamics of photogenerated electrons and holes cannot be adequately described within a single-particle picture as excitonic effects also impact the polarization dynamics of the optical transitions. As previously discussed and predicted in Refs. (Cao [et al.](#page-24-6), [2012;](#page-24-6) [Xiao](#page-28-6) [et al.](#page-28-6), [2012\)](#page-28-6), optical valley initialization is based on chiral selection rules for interband transitions: σ^+ polarized excitation results in the inter-band transitions in the K^+ valley, and, correspondingly, σ^- polarized excitation results in transitions in the K^- valley. Initial experimental confirmation of this effect was reported in steady-state PL measurements in $MoS₂$ monolayers [\(Cao](#page-24-6) [et al.](#page-24-6), [2012;](#page-24-6) Mak [et al.](#page-26-16), [2012;](#page-26-16) [Sallen](#page-27-8) et al., [2012;](#page-27-8) [Zeng](#page-29-9) $et al., 2012$ $et al., 2012$), as well as in $WSe₂$ and $WS₂$ systems [\(Jones](#page-25-44) [et al.](#page-25-44), [2013;](#page-25-44) Kim [et al.](#page-25-47), [2014;](#page-25-47) Mai [et al.](#page-26-40), [2014b;](#page-26-40) Sie [et al.](#page-27-41), [2015b;](#page-27-41) [Wang](#page-28-33) et al., [2014;](#page-28-33) Zhu [et al.](#page-29-16), [2014a\)](#page-29-16). The overall degree of polarization has been shown to reach almost unity. In ML MoSe₂, however, non-resonant excitation usually results in at most 5% PL polarization [\(Wang](#page-28-42) [et al.](#page-28-42), [2015b\)](#page-28-42), the reason for this difference remaining a topic of ongoing discussion. Interestingly, for $MoSe₂$, the application of a strong out-of-plane magnetic field combined with resonant or nearly resonant optical excitation appears to be necessary to initialize large valley polarization [\(Kioseoglou](#page-25-48) et al., [2016\)](#page-25-48). Finally, in addition to optical valley initialization, strong circularly polarized emission is also reported from electro-luminescence in TMD-based light-emitting devices – an interesting and technologically promising observation [\(Onga](#page-26-41) et al., [2016;](#page-26-41) [Yang](#page-28-43) et al., [2016;](#page-28-43) [Zhang](#page-29-22) et al., [2014c\)](#page-29-22).

As previously discussed in Sec. [II,](#page-7-0) following excitation with circularly polarized light across the band gap, an exciton is formed from carriers in a specific K valley due to the robust, valley dependent optical selection rules. The degree of circular polarization P_c , as measured in steady state PL, can be approximated as $P_c = P_0/(1 + \tau/\tau_s)$, where τ is exciton lifetime, τ_s is the polarization lifetime and P_0 is the initially generated polarization. High P_c in steady state PL experiments generally results from a specific ratio of τ versus τ_s and does not necessary require particularly long polarization lifetimes. Hence the extrinsic parameters such as, e.g., short carrier lifetimes due to non-radiative channels can strongly affect this value and detailed analysis of steady-state experiments is challenging.

Time-resolved studies provide more direct access to the valley dynamics of excitons. In particular, the determination of the exciton PL emission times on the order of several to tens of picoseconds in typical samples at low temperature, together with measurements of the polarization dynamics indicate that the neutral exciton looses its initial valley polarization very quickly, over a few ps. This observation is difficult to understand at the level of individual electrons and holes: The valley polarization in TMDs monolayers should be very stable from within single-particle picture as it requires inter-valley scattering with change in momentum, typically combined with additional electron and hole spin flipping (Xiao [et al.](#page-28-6), [2012\)](#page-28-6). Spin conserving inter-valley scattering is generally energetically unfavorable due to spin splittings of several

hundreds and tens of meV in the valence and conduction bands, respectively [\(Kormanyos](#page-25-4) et al., [2015\)](#page-25-4). In considering the valley dynamics following optical excitation, it is, however, crucial to note that rather than observing individual spin and valley polarized carriers, we create and probe the dynamics of valley-polarized excitons.

The Coulomb interaction between the charge carriers does, in fact, strongly impact the valley dynamics in TMD MLs: The long-range exchange interaction between the electron and hole forming an exciton gives rise to a new and efficient decay mechanism for the exciton polarization [\(Glazov](#page-25-12) et al., [2014;](#page-25-12) Hao [et al.](#page-25-49), [2016;](#page-25-49) [Yu](#page-29-23) [et al.](#page-29-23), [2014;](#page-29-23) [Yu and Wu,](#page-29-24) [2014;](#page-29-24) Zhu [et al.](#page-29-20), [2014b\)](#page-29-20). Indeed, the $k \cdot p$ -interaction results in the admixture of the valence band states in the conduction electron state and of the conduction band states in the hole state in the exciton. As a result of this admixture and of the Coulomb interaction, an exciton with an electron in the K^+ valley can effectively recombine and produce to an exciton with an electron in the K^- valley. This process needs neither the transfer of significant momentum of an individual carrier nor its spin flip. It can be interpreted in a purely electrodynamical way if one considers an optically active exciton as a microscopic dipole oscillating at its resonant frequency. Naturally, this mechanism is efficient only for bright exciton states and the dark states are largely unaffected. For a bright exciton propagating in the ML plane with the center of mass wavevector K_{exc} , the proper eigenstates are the linear combinations of states active in the σ^+ and σ^- circular polarization: One eigenstate has a microscopic dipole moment oscillating along the wavevector K_{exc} , this is the longitudinal exciton, and the other one has the dipole moment oscillating perpendicular to the K_{exc} , being the transverse exciton. The splitting between those states, i.e., the longitudinal-transverse splitting, acts as an effective magnetic field and mixes the σ^+ and σ^- polarized excitons, which are no longer eigenstates of the system, leading to depolarization of excitons [\(Glazov](#page-25-12) et al., [2014,](#page-25-12) [2015;](#page-25-13) [Ivchenko,](#page-25-17) [2005;](#page-25-17) [Maialle](#page-26-9) et al., [1993\)](#page-26-9). As compared with other 2D excitons, e.g., in GaAs or CdTe quantum wells, in TMD MLs the longitudinal-transverse splitting is enhanced by one to two orders of magnitude due to the tighter binding of the electron to the hole in the exciton and, correspondingly, the much higher oscillator strength of the optical transitions (Li [et al.](#page-26-42), [2014a\)](#page-26-42). This enhanced longitudinal-transverse splitting as compared to GaAs quantum wells leads to a comparatively faster exciton polarization relaxation. This mechanism, here discussed in the context of valley polarization, also limits valley coherence times [\(Glazov](#page-25-12) et al., [2014;](#page-25-12) [Hao](#page-25-49) $et al., 2016$ $et al., 2016$, see below.

Experimentally, the valley polarization dynamics can be monitored by polarization-resolved time-resolved photoluminescence (TRPL) and pump-probe measurements. By using time-resolved Kerr rotation, Zhu et al. found that in monolayer $WSe₂$ the exciton valley depolarization time is around 6 ps at 4K, in good agreement with

FIG. 7 (a) Exciton PL emission time of the order of 2 ps measured in time-resolved photo-luminescence for ML WSe₂ at $T = 7$ K [\(Robert](#page-27-23) *et al.*, [2016\)](#page-27-23). (b) Schematic showing that $|+1\rangle$ and $|-1\rangle$ neutral excitons are coupled by the electron-hole Coulomb exchange interaction [\(Glazov](#page-25-12) *et al.*, [2014\)](#page-25-12). (c) Decay of the **neutral exciton** polarization in WSe₂ monolayers on ps time scales as measured by Kerr rotation (Zhu [et al.](#page-29-20), [2014b\)](#page-29-20) (d) Decay of resident electron polarization as measured by Kerr rotation in monolayer WS₂, with a typical time constant of 5 ns [\(Bushong](#page-24-40) *et al.*, [2016\)](#page-24-40) for $T = 6$ K. (e) Decay of **hole** polarization in a charge tunable WSe₂ monolayer with a time constant of $2\mu s$ (Dey *[et al.](#page-25-50),* [2017\)](#page-25-50) for $T = 4$ K, where B_y is the magnetic field applied in the sample plane.

the Coulomb exchange mediated valley depolarization (Yan [et al.](#page-28-44), [2017;](#page-28-44) Zhu [et al.](#page-29-20), [2014b\)](#page-29-20), see Fig. [7c](#page-21-1). In ML $MoS₂$ and $MoSe₂$ fast exciton depolarization times $(\approx$ ps) were also reported [\(Jakubczyk](#page-25-30) *et al.*, [2016;](#page-25-30) [La](#page-26-38)[garde](#page-26-38) et al., [2014;](#page-26-38) Mai [et al.](#page-26-39), [2014a;](#page-26-39) [Wang](#page-28-40) et al., [2013\)](#page-28-40). All these experiments demonstrate measurable depolarization of the neutral exciton X^0 , although the exact relaxation time may be different in specific measurements depending on the samples used, experimental conditions and techniques employed.

Valley depolarization due to the long-range Coulomb exchange is expected to be less efficient for spatially indirect excitons, where the electron-hole overlap is weaker. This configuration applies to type II ML TMD heterostructures, where holes reside in WSe_2 and electrons in MoSe2, for example. Indeed [Rivera](#page-27-42) et al. [\(2015\)](#page-27-42); [Rivera](#page-27-43) [et al.](#page-27-43) [\(2016\)](#page-27-43) have observed valley lifetimes of tens of ns for indirect excitons at low temperature, which motivates further valley dynamics experiments in structures with tunable Coulomb interactions, albeit with more complex polarization selection rules. Another type of excitons that is, in principle, unaffected by valley depolarization through Coulomb exchange are optically dark excitons. With a slight mixing of bright excitons with dark excitons (for optical readout), the dark excitons may provide a promising alternative configuration for exciton valley

manipulation [\(Zhang](#page-29-7) *et al.*, [2017\)](#page-29-7).

In addition to the role of Coulomb exchange effects on valley polarization, other mechanisms linked to disorder in the sample and the associated scattering with impurities and phonons have also been investigated, with further details in [\(McCreary](#page-26-43) et al., [2017;](#page-26-43) [Neumann](#page-26-44) et al., [2017;](#page-26-44) Tran [et al.](#page-28-15), [2017;](#page-28-15) [Yu and Wu,](#page-29-25) [2016\)](#page-29-25).

B. Valley coherence

As discussed in the previous section, excitation with circularly polarized light can induce valley polarization in a TMD monolayer (Xiao [et al.](#page-28-6), [2012\)](#page-28-6). Similarly, excitation with linearly polarized light can generate valley coherence, i.e., a *coherent* superposition of K^+ and $K^$ valley states, as first reported for the neutral exciton in ML WSe₂ [\(Jones](#page-25-44) *et al.*, [2013\)](#page-25-44). A fingerprint of generated valley coherence is the emission of linearly polarized light from the neutral exciton, polarized along the same axis as the polarization of the excitation, an effect also termed optical alignment of excitons in the earlier literature [\(Meier and Zakharchenya,](#page-26-45) [1984\)](#page-26-45). In addition, valley coherence in the ML is sufficiently robust to allow rotation of the coherent superposition of valley states in applied magnetic fields [\(Cadiz](#page-24-15) et al., [2017;](#page-24-15) [Schmidt](#page-27-44) et al., [2016a;](#page-27-44) [Wang](#page-28-45) et al., [2016a\)](#page-28-45) or with the help of a pseudomagnetic field generated by circularly polarized light via the optical Stark effect (Ye [et al.](#page-28-46), [2017\)](#page-28-46).

C. Valley polarization dynamics of trions and free charge carriers

For manipulating valley polarization of bright, direct excitons within the radiative cone, the radiative lifetime in the ps range sets an upper bound for the available time scale. In addition neutral exciton valley polarization of the neutral exciton decays rapidly due to the Coulomb-exchange mediated mechanism discussed above and shown in Fig. [7c](#page-21-1). This depolarization mechanism does not apply to single carriers for which spin-valley locking due to the large spin-orbit spin splittings is expected to lead to significantly longer polarization lifetimes. In the presence of resident carriers, optical excitation can lead to the formation of charged excitons also called trions, Sec. [III.B.](#page-18-0) Commonly observed bright trions decay on slightly longer timescales than excitons, namely in about 30 ps at $T = 4$ K [\(Wang](#page-28-33) *et al.*, [2014\)](#page-28-33), which means that the time range for valley index manipulation is still restricted to ultra-fast optics. For future valleytronics experiments and devices, it is therefore interesting to know whether the resident carriers left behind after recombination are spin and valley polarized.

Several recent time-resolved studies point to encouragingly long polarization dynamics of resident carriers in monolayer TMDs at low temperature. Polarization decays of $3-5$ ns were observed in CVD-grown $MoS₂$ and WS_2 monolayers that were unintentionally electrondoped [\(Bushong](#page-24-40) et al., [2016;](#page-24-40) Yang [et al.](#page-28-47), [2015a](#page-28-47)[,b\)](#page-28-48), as can be seen in Fig. [7d](#page-21-1). Longer times up to tens of ns were observed in unintentionally hole-doped CVD-grown $WSe₂$ (Hsu *[et al.](#page-27-45)*, [2015;](#page-25-51) Song *et al.*, [2016\)](#page-27-45). Using timeresolved Kerr rotation, the spin/valley dynamics of resident electrons and holes in charge-tunable $WSe₂$ monolayer were recenty measured by Dey [et al.](#page-25-50) [\(2017\)](#page-25-50). In the n-type regime, long (∼70 ns) polarization relaxation of electrons were observed and considerably longer ($\sim 2 \mu s$) polarization relaxation of holes were revealed in the pdoped regime (see Fig. [7e](#page-21-1)), as expected because of the strong spin-valley locking of holes in the valence band of monolayer TMDs. Long hole polarization lifetimes were also suggested by a recent report of microsecond hole polarizations of indirect excitons in WSe_2/MoS_2 bilayers (Kim [et al.](#page-25-52), [2016\)](#page-25-52). In this case rapid electron-hole spatial separation following neutral exciton generation leads to long-lived indirect excitons, in which the spatial overlap of the electron and hole is relatively small. If the two layers are not aligned with respect to the inplane angle, there is also an additional mismatch of the respective band extrema in momentum space (Yu [et al.](#page-29-26), [2015c\)](#page-29-26). The resulting oscillator strength is very small and should directly lead to a rather slow spin-valley depolarization through long-range exchange coupling, previously

FIG. 8 (a) Schematic of Zeeman shifts in magnetic field \boldsymbol{B} perpendicular to the monolayer plane. (b) Measurements on $MoSe₂ MLs from (MacNeil *et al.*, 2015) that show a clear$ $MoSe₂ MLs from (MacNeil *et al.*, 2015) that show a clear$ $MoSe₂ MLs from (MacNeil *et al.*, 2015) that show a clear$ Zeeman splitting. (c) Reflectivity measurements on WS_2 MLs in high magnetic fields and (d) the Zeeman splitting extracted for A- and B-excitons (Stier [et al.](#page-28-24), [2016a\)](#page-28-24).

discussed in Sec. [IV.A.](#page-19-1) One of the most important challenges at this early stage is to identify the conditions and mechanisms that promote transfer of the optical generated valley polarization of trions or neutral excitons to the resident carriers [\(Dyakonov,](#page-25-8) [2008;](#page-25-8) [Glazov,](#page-25-53) [2012\)](#page-25-53).

D. Lifting valley degeneracy in external fields

In the absence of any external or effective magnetic or electric field, the exciton transitions involving carriers in the K^+ and K^- valley are degenerate and the spin states in the two types of valleys are related by time reversal symmetry. This symmetry can be broken through the application of an external magnetic field perpendicular to the plane of the monolayer. There are two important consequences that are briefly discussed below: first, the valley states split by a Zeeman energy ΔE_Z typically on the order of a few meV at 10 Tesla. Second, the valley polarization could change due to this splitting, as the lower energy valley might be populated preferentially.

Application of a magnetic field B_z along the z direction (perpendicular to the ML plane) gives rise to a valley Zeeman splitting in monolayer WSe_2 and $MoSe_2$ [\(Aivazian](#page-24-41) [et al.](#page-24-41), [2015;](#page-24-41) Li [et al.](#page-26-47), [2014b;](#page-26-47) [MacNeill](#page-26-46) et al., [2015;](#page-26-46) [Sri](#page-27-46)[vastava](#page-27-46) et al., [2015;](#page-27-46) [Wang](#page-28-49) et al., [2015\)](#page-28-49), lifting the valley degeneracy. In these studies, an energy difference ΔE_Z on the meV scale is found between the σ^+ and σ^- polarized PL components, stemming from the K^+ (K^-) valley, respectively, as $\Delta E_Z = E(\sigma^+) - E(\sigma^-)$. In monolayer MoSe₂, the σ^+ and σ^- PL components are clearly split in magnetic fields of 6.7 T as shown in Fig. [8](#page-22-2) [\(MacNeill](#page-26-46)

[et al.](#page-26-46), [2015\)](#page-26-46). The valley Zeeman splitting scales linearly with the magnetic field as depicted in Fig. [8](#page-22-2) and the slope gives the effective exciton g-factor as $\Delta E_Z = g_X \mu_B B_z$, where μ_B is the Bohr magneton. The exciton g-factor g_X measured for instance in PL contains contribution from electron and hole g-factors. In several magneto-optics experiments also on ML MoTe₂ and WS₂ [\(Arora](#page-24-42) *et al.*, [2016;](#page-24-42) [Mitioglu](#page-26-48) et al., [2015,](#page-26-48) [2016;](#page-26-49) Stier [et al.](#page-28-24), [2016a\)](#page-28-24) the exciton q -factor is about -4 . The exact energy separation of the valley and spin states is important for spin and valley manipulation schemes. In addition, the q -factor also contains important information on the impact of remote bands on the optical transitions, in a similar way as the effective mass tensor, see discussions in [MacNeill](#page-26-46) $et \ al. (2015)$ $et \ al. (2015)$; [Wang](#page-28-49) $et \ al. (2015)$. The origin of this large g-factor is currently not fully understood. There are basically two approaches to calculate the Zeeman splittings in TMD MLs. One is based on the atomic approach by considering atoms as essentially isolated and associating the g-factors of the conduction and valence band states with the spin and orbital contributions of corresponding d_{z^2} and $d_{(x\pm iy)^2}$ atomic shells [\(Aivazian](#page-24-41) *et al.*, [2015;](#page-24-41) [Sri](#page-27-46)[vastava](#page-27-46) et al., [2015\)](#page-27-46). The other approach is based on the Bloch theorem and $\mathbf{k} \cdot \mathbf{p}$ -perturbation theory which allows to relate g-factor with the band structure parameters of TMD ML [\(MacNeill](#page-26-46) et al., [2015\)](#page-26-46). Merging these approaches, which can be naturally done within atomistic tight-binding models [\(Rybkovskiy](#page-27-47) et al., [2017;](#page-27-47) [Wang](#page-28-49) [et al.](#page-28-49), [2015\)](#page-28-49), is one of the open challenges for further theoretical studies.

At zero magnetic field, the valley polarization in optical experiments is only induced by the circularly polarized excitation laser. At finite magnetic fields, a valley Zeeman splitting is induced and the observed polarization may now also depend on the magnetic field strength. For ML WSe₂, sign and amplitude of the valley polarization, even in magnetic fields of several Tesla, is mainly determined by the excitation laser helicity [\(Mitioglu](#page-26-48) et al., [2015;](#page-26-48) [Wang](#page-28-49) et al., [2015\)](#page-28-49). In contrast, the sign and amplitude of the valley polarization detected via PL emission in $MoSe₂$ and $MoTe₂$ is mainly determined by the sign and amplitude of the applied magnetic field [\(Arora](#page-24-42) et al., [2016;](#page-24-42) [MacNeill](#page-26-46) et al., [2015;](#page-26-46) [Wang](#page-28-49) et al., [2015\)](#page-28-49).

In contrast to a perpendicular magnetic field, in monolayer MoS₂ an *in-plane* magnetic field (xy) up to 9 T does not measurably affect the exciton valley polariza-tion or splitting [\(Sallen](#page-27-8) *[et al.](#page-29-9)*, [2012;](#page-27-8) Zeng *et al.*, [2012\)](#page-29-9), as expected from symmetry arguments. The in-plane field, however, mixed spin-up and spin-down states in the conduction and valence bands and activates spinforbidden excitons as discussed above in Sec. [II.C.1](#page-14-1) and in Refs. [\(Molas](#page-26-15) et al., [2017;](#page-26-15) [Zhang](#page-29-7) et al., [2017\)](#page-29-7).

An elegant, alternative way of lifting valley degeneracy is using the optical Stark effect. Typically a circularly polarized pulsed laser with below bandgap radiation is used to induce a shift in energy of the exciton resonance [\(Jof](#page-25-54)fre [et al.](#page-25-54), [1989;](#page-25-54) [Press](#page-27-48) et al., [2008\)](#page-27-48). This shift becomes valley selective in ML TMDs, with induced effective Zeeman splitting is up to ≈ 20 meV, corresponding to effective magnetic fields of tens of Tesla (Kim [et al.](#page-25-47), [2014;](#page-25-47) Sie *[et al.](#page-27-41)*, [2015b\)](#page-27-41). The effective magnetic field created by the Stark effect can also be employed to rotate a coherent superposition of valley states (Ye [et al.](#page-28-46), [2017\)](#page-28-46).

V. SUMMARY AND PERSPECTIVES

In this short review we have detailed some of the remarkable optical properties of transition metal dichalcogenide monolayers. The strong Coulomb interaction leads to exciton binding energies of several hundred meV and excitons therefore dominate the optical properties up to room temperature. The ultimate thinness of these materials provides unique opportunities for engineering the excitonic properties. For example, the dielectric environment can be tuned. Here first experiments show that encapsulation of TMD monolayers in hexagonal boron nitride, for example, significantly reduces the exciton binding energy (Stier [et al.](#page-28-24), [2016a\)](#page-28-24). More experiments will show in the future how sensitive the exciton ground, excited states and the free carrier bandgap are to changes in their dielectric environment (Raja [et al.](#page-27-13), [2017;](#page-27-13) Ye [et al.](#page-28-22), [2014\)](#page-28-22), which will depend on the spatial extent of the different states.

Another route to engineering the optical properties, particularly the polarization dynamics, is to place ferromagnetic layers close to the monolayer. These proximity effects might be able to lift valley degeneracy even without applying any external magnetic fields, a great prospect for controlling spin and valley dynamics [\(Zhao](#page-29-27) [et al.](#page-29-27), [2016;](#page-29-27) [Zhong](#page-29-28) et al., [2017\)](#page-29-28).

In this article we have concentrated on excitons in single monolayers, but many of these concepts apply also to more complex exciton configurations in van der Waals heterostructures [\(Geim and Grigorieva,](#page-25-0) [2013\)](#page-25-0) where the electrons and holes do not necessarily reside in the same layer. Here many possibilities can be explored, such as studies of Bose-Einstein condensates and superfluidity; the wide choice of layered materials allows tuning the oscillator strength of the optical transitions as well as the spin- and valley polarization lifetimes [\(Ceballos](#page-24-43) et al., [2014;](#page-24-43) [Fogler](#page-25-40) et al., [2014;](#page-25-40) Kim [et al.](#page-25-52), [2016;](#page-25-52) [Nagler](#page-26-50) et al., [2017;](#page-26-50) [Rivera](#page-27-43) et al., [2016\)](#page-27-43).

Acknowledgments

G.W. and B.U. acknowledge funding from ERC Grant No. 306719. A.C. gratefully acknowledges funding by the Deutsche Forschungsgemeinschaft (DFG) through the Emmy Noether Programme (CH 1672/1-1). M.M.G. acknowledges support through RF President grant MD-1555.2017.2 and RFBR projects 17-02-00383 and 17-52- 16020. T.F.H. wishes to acknowledge support through the AMOS program within the Chemical Sciences, Geosciences, and Biosciences Division, Office of Basic Energy Sciences of the U.S. Department of Energy under Contract No. DE-AC02-76-SFO0515 and by the Gordon and Betty Moore Foundations EPiQS Initiative through Grant No. GBMF4545. X.M. and T.A. thank ANR MoS2ValleyControl. X.M. also acknowledges the Institut Universitaire de France. M.G, X. M. B.U and T.A. acknowledge the LIA CNRS-Ioffe ILNACS.

We thank group members and colleagues, past and present, for stimulating discussions, in particular T. Berkelbach, D. Reichman, C. Robert, I.C. Gerber, M.V. Durnev, M.A. Semina and E.L. Ivchenko.

*present address G.W.: Cambridge Graphene Centre, University of Cambridge, Cambridge CB3 0FA, UK

References

- Adamyan, V. M., O. A. Smyrnov, and S. V. Tishchenko, 2008, Journal of Physics: Conference Series 129(1), 012012.
- Aivazian, G., Z. Gong, A. M. Jones, R.-L. Chu, J. Yan, D. G. Mandrus, C. Zhang, D. Cobden, W. Yao, and X. Xu, 2015, Nature Physics 11, 148.
- Ajayi, O., J. Ardelean, G. Shepard, J. Wang, A. Antony, T. Taniguchi, K. Watanabe, T. Heinz, S. Strauf, X. Zhu, et al., 2017, 2D Materials .
- Amand, T., B. Dareys, B. Baylac, X. Marie, J. Barrau, M. Brousseau, D. J. Dunstan, and R. Planel, 1994, Phys. Rev. B 50, 11624.
- Amani, M., D.-H. Lien, D. Kiriya, J. Xiao, A. Azcatl, J. Noh, S. R. Madhvapathy, R. Addou, K. Santosh, M. Dubey, $et \ al., 2015, Science \ 350(6264), 1065.$
- Ando, T., 2010, Journal of the Physical Society of Japan 79(2), 024706.
- Andreani, L. C., 1995, Confined electrons and photons. New physics and applications (NATO ASI), chapter Optical transitions, excitons, and polaritons in bulk and lowdimensional semiconductor structures, NATO ASI Series.
- Andreani, L. C., F. Tassone, and F. Bassani, 1991, Solid State Communications 77(9), 641 .
- Arora, A., M. Koperski, K. Nogajewski, J. Marcus, C. Faugeras, and M. Potemski, 2015a, Nanoscale 7(23), 10421.
- Arora, A., K. Nogajewski, M. Molas, M. Koperski, and M. Potemski, 2015b, Nanoscale 7(48), 20769.
- Arora, A., R. Schmidt, R. Schneider, M. R. Molas, I. Breslavetz, M. Potemski, and R. Bratschitsch, 2016, Nano Letters 0, 10.1021/acs.nanolett.6b00748.
- Ayari, A., E. Cobas, O. Ogundadegbe, and M. S. Fuhrer, 2007, Journal of Applied Physics 101(1), 014507.
- Baranowski, M., A. Surrente, D. K. Maude, M. Ballottin, A. A. Mitioglu, P. C. M. Christianen, Y. C. Kung, D. Dumcenco, A. Kis, and P. Plochocka, 2017, 2D Materials 4(2), 025016.
- Barrau, J., M. Heckmann, and M. Brousseau, 1973, Journal of Physics and Chemistry of Solids 34(3), 381 , ISSN 0022- 3697.
- Behnia, K., 2012, Nature nanotechnology 7(8), 488.
- Berestetskii, V. B., and L. D. Landau, 1949, Zh. Eksp. Teor. Fiz 19, 673.
- Berghauser, G., A. Knorr, and E. Malic, 2017, 2D Materials 4(1), 015029.
- Berghäuser, G., and E. Malic, 2014, Phys. Rev. B 89, 125309.
- Berkelbach, T. C., M. S. Hybertsen, and D. R. Reichman, 2013, Phys. Rev. B 88, 045318.
- Berkelbach, T. C., M. S. Hybertsen, and D. R. Reichman, 2015, Physical Review B 92(8), 085413, ISSN 1098-0121.
- Bir, G. L., and G. E. Pikus, 1974, Symmetry and Straininduced Effects in Semiconductors (Wiley/Halsted Press).
- Bonnot, A., R. Planel, and C. B. à la Guillaume, 1974, Phys. Rev. B 9, 690.
- Bradford, C., C. O'Donnell, B. Urbaszek, C. Morhain, A. Balocchi, K. Prior, and B. Cavenett, 2001, Physical Review B 64(19), 195309.
- Bradley, A. J., M. M. Ugeda, F. H. da Jornada, D. Y. Qiu, W. Ruan, Y. Zhang, S. Wickenburg, A. Riss, J. Lu, S.- K. Mo, Z. Hussain, Z.-X. Shen, et al., 2015, Nano Letters $15(4)$, 2594.
- Bromley, R., R. Murray, and A. Yoffe, 1972, Journal of Physics C: Solid State Physics 5(7), 759.
- Bushong, E. J., Yunqiu, Luo, K. M. McCreary, M. J. Newburger, S. Singh, B. T. Jonker, and R. K. Kawakami, 2016, ArXiv e-prints eprint 1602.03568.
- Butler, S. Z., S. M. Hollen, L. Cao, Y. Cui, J. A. Gupta, H. R. Gutiérrez, T. F. Heinz, S. S. Hong, J. Huang, A. F. Ismach, E. Johnston-Halperin, M. Kuno, et al., 2013, ACS Nano 7(4), 2898.
- Cadiz, F., E. Courtade, C. Robert, G. Wang, Y. Shen, H. Cai, T. Taniguchi, K. Watanabe, H. Carrere, D. Lagarde, M. Manca, T. Amand, et al., 2017, Phys. Rev. X 7, 021026.
- Cao, T., G. Wang, W. Han, H. Ye, C. Zhu, J. Shi, Q. Niu, P. Tan, E. Wang, B. Liu, and J. Feng, 2012, Nature Communications 3, 887.
- Castellanos-Gomez, A., 2016, Nature Photonics 10(4), 202.
- Castellanos-Gomez, A., M. Buscema, R. Molenaar, V. Singh, L. Janssen, H. S. J. van der Zant, and G. A. Steele, 2014, 2D Materials 1(1), 011002.
- Ceballos, F., M. Z. Bellus, H.-Y. Chiu, and H. Zhao, 2014, ACS nano 8(12), 12717.
- Ceballos, F., Q. Cui, M. Z. Bellus, and H. Zhao, 2016, Nanoscale 8(22), 11681.
- Cha, S., J. H. Sung, S. Sim, J. Park, H. Heo, M.-H. Jo, and H. Choi, 2016, Nature communications 7, 10768.
- Chaves, A. J., R. M. Ribeiro, T. Frederico, and N. M. R. Peres, 2017, 2D Materials 4(2), 025086.
- Cheiwchanchamnangij, T., and W. R. L. Lambrecht, 2012, Phys. Rev. B 85, 205302.
- Cheng, R., D. Li, H. Zhou, C. Wang, A. Yin, S. Jiang, Y. Liu, Y. Chen, Y. Huang, and X. Duan, 2014, Nano Letters $14(10)$, 5590.
- Chernikov, A., T. C. Berkelbach, H. M. Hill, A. Rigosi, Y. Li, O. B. Aslan, D. R. Reichman, M. S. Hybertsen, and T. F. Heinz, 2014, Phys. Rev. Lett. 113, 076802.
- Chernikov, A., C. Ruppert, H. M. Hill, A. F. Rigosi, and T. F. Heinz, 2015a, Nature Photonics 9(7), 466.
- Chernikov, A., A. M. van der Zande, H. M. Hill, A. F. Rigosi, A. Velauthapillai, J. Hone, and T. F. Heinz, 2015b, Phys. Rev. Lett. 115, 126802.
- Chichibu, S., T. Azuhata, T. Sota, and S. Nakamura, 1996, Applied Physics Letters 69(27), 4188.
- Chiu, M.-H., C. Zhang, H.-W. Shiu, C.-P. Chuu, C.-H. Chen, C.-Y. S. Chang, C.-H. Chen, M.-Y. Chou, C.-K. Shih, and L.-J. Li, 2015, Nature communications 6.
- Chow, C. M., H. Yu, A. M. Jones, J. R. Schaibley, M. Koehler, D. G. Mandrus, R. Merlin, W. Yao, and X. Xu, 2017, ArXiv e-prints eprint 1701.02770.
- Citrin, D. S., 1993, Phys. Rev. B 47, 3832.
- Coleman, J. N., M. Lotya, A. ONeill, S. D. Bergin, P. J. King, U. Khan, K. Young, A. Gaucher, S. De, R. J. Smith, et al., 2011, Science 331(6017), 568.
- Courtade, E., M. Semina, M. Manca, M. M. Glazov, C. Robert, F. Cadiz, G. Wang, T. Taniguchi, K. Watanabe, M. Pierre, W. Escoffier, E. L. Ivchenko, et al., 2017, Phys. Rev. B 96, 085302.
- Crooker, S. A., T. Barrick, J. A. Hollingsworth, and V. I. Klimov, 2003, Applied Physics Letters 82(17), 2793.
- Cudazzo, P., I. V. Tokatly, and A. Rubio, 2011, Phys. Rev. B 84, 085406.
- Denisov, M. M., and V. P. Makarov, 1973, Physica Status Solidi (b) 56(1), 9.
- Dery, H., 2016, Phys. Rev. B 94, 075421.
- Dery, H., and Y. Song, 2015, Phys. Rev. B 92, 125431.
- Deslippe, J., M. Dipoppa, D. Prendergast, M. V. O. Moutinho, R. B. Capaz, and S. G. Louie, 2009, Nano Letters 9(4), 1330.
- Deveaud, B., F. Clérot, N. Roy, K. Satzke, B. Sermage, and D. S. Katzer, 1991, Phys. Rev. Lett. 67, 2355.
- Dey, P., J. Paul, Z. Wang, C. E. Stevens, C. Liu, A. H. Romero, J. Shan, D. J. Hilton, and D. Karaiskaj, 2016, Phys. Rev. Lett. 116, 127402.
- Dey, P., L. Yang, C. Robert, G. Wang, B. Urbaszek, X. Marie, and S. A. Crooker, 2017, ArXiv e-prints eprint 1704.05448.
- Van der Donck, M., M. Zarenia, and F. M. Peeters, 2017, Phys. Rev. B 96, 035131.
- Dufferwiel, S., S. Schwarz, F. Withers, A. Trichet, F. Li, M. Sich, O. Del Pozo-Zamudio, C. Clark, A. Nalitov, D. Solnyshkov, et al., 2015, Nature communications 6, 8579.
- Dyakonov, M., 2008, Springer Series in Solid-State Science, Springer-Verlag Berlin 157.
- Echeverry, J. P., B. Urbaszek, T. Amand, X. Marie, and I. C. Gerber, 2016, Phys. Rev. B 93, 121107.
- Efimkin, D. K., and A. H. MacDonald, 2017, Phys. Rev. B 95, 035417.
- Flatten, L. C., Z. He, D. M. Coles, A. A. Trichet, A. W. Powell, R. A. Taylor, J. H. Warner, and J. M. Smith, 2016, Scientific Reports 6, 33134.
- Fogler, M. M., L. V. Butov, and K. S. Novoselov, 2014, Nat Commun 5, 10.1038/ncomms5555.
- Frindt, R. F., 1966, Journal of Applied Physics 37(4), 1928.
- Ganchev, B., N. Drummond, I. Aleiner, and V. Fal'ko, 2015, Phys. Rev. Lett. 114, 107401.
- Geim, A. K., and I. V. Grigorieva, 2013, Nature 499, 419.
- Glazov, M., 2012, Physics of the Solid State $54(1)$, 1.
- Glazov, M. M., T. Amand, X. Marie, D. Lagarde, L. Bouet, and B. Urbaszek, 2014, Phys. Rev. B 89, 201302.
- Glazov, M. M., L. E. Golub, G. Wang, X. Marie, T. Amand, and B. Urbaszek, 2017, Phys. Rev. B 95, 035311.
- Glazov, M. M., E. L. Ivchenko, G. Wang, T. Amand, X. Marie, B. Urbaszek, and B. L. Liu, 2015, physica status solidi (b) 252(11), 2349, ISSN 1521-3951.
- Gong, P., H. Yu, Y. Wang, and W. Yao, 2017, Phys. Rev. B 95, 125420.
- Goupalov, S. V., E. L. Ivchenko, and A. V. Kavokin, 1998, Sov. Phys.–JETP 86, 388.
- Hanbicki, A., M. Currie, G. Kioseoglou, A. Friedman, and B. Jonker, 2015, Solid State Communications 203(0), 16 .
- Hao, K., G. Moody, F. Wu, C. K. Dass, L. Xu, C.-H. Chen, M.-Y. Li, L.-J. Li, A. H. MacDonald, and X. Li, 2016, Nature Physics doi:10.1038/nphys3674 .
- Haug, H., and S. W. Koch, 2009, Quantum theory of the optical and electronic properties of semiconductors (World Scientific, Singapore), 5th edition.
- He, K., N. Kumar, L. Zhao, Z. Wang, K. F. Mak, H. Zhao, and J. Shan, 2014, Phys. Rev. Lett. 113, 026803.
- Hill, H. M., A. F. Rigosi, C. Roquelet, A. Chernikov, T. C. Berkelbach, D. R. Reichman, M. S. Hybertsen, L. E. Brus, and T. F. Heinz, 2015, Nano letters 15(5), 2992.
- Hsu, W.-T., Y.-L. Chen, C.-H. Chen, P.-S. Liu, T.-H. Hou, L.-J. Li, and W.-H. Chang, 2015, Nature communications 6.
- Ivchenko, E. L., 2005, Optical spectroscopy of semiconductor nanostructures (Alpha Science, Harrow UK).
- Jakubczyk, T., V. Delmonte, M. Koperski, K. Nogajewski, C. Faugeras, W. Langbein, M. Potemski, and J. Kasprzak, 2016, Nano Letters 16(9), 5333.
- Jin, C., J. Kim, J. Suh, Z. Shi, B. Chen, X. Fan, M. Kam, K. Watanabe, T. Taniguchi, S. Tongay, et al., 2016, Nature Physics .
- Jin, C., J. Kim, K. Wu, B. Chen, E. S. Barnard, J. Suh, Z. Shi, S. G. Drapcho, J. Wu, P. J. Schuck, S. Tongay, and F. Wang, 2017, Advanced Functional Materials 27(19), 1601741.
- Joensen, P., R. F. Frindt, and S. R. Morrison, 1986, Mat. Res. Bull. 21(4), 457.
- Joffre, M., D. Hulin, A. Migus, and M. Combescot, 1989, Phys. Rev. Lett. 62, 74.
- Jones, A. M., H. Yu, N. J. Ghimire, S. Wu, G. Aivazian, J. S. Ross, B. Zhao, J. Yan, D. G. Mandrus, D. Xiao, W. Yao, and X. Xu, 2013, Nat. Nanotechnol. 8, 634.
- Jones, A. M., H. Yu, J. R. Schaibley, J. Yan, D. G. Mandrus, T. Taniguchi, K. Watanabe, H. Dery, W. Yao, and X. Xu, 2016, Nat Phys 12(4), 323.
- Keldysh, L. V., 1979, Soviet Journal of Experimental and Theoretical Physics Letters 29, 658.
- Keldysh, L. V., and A. N. Kozlov, 1968, Sov. Phys. JETP 27, 521.
- Kheng, K., R. T. Cox, M. Y. d' Aubigné, F. Bassani, K. Saminadayar, and S. Tatarenko, 1993, Phys. Rev. Lett. 71, 1752.
- Kim, J., X. Hong, C. Jin, S.-F. Shi, C.-Y. S. Chang, M.- H. Chiu, L.-J. Li, and F. Wang, 2014, Science 346(6214), 1205.
- Kim, J., C. Jin, B. Chen, H. Cai, T. Zhao, P. Lee, S. Kahn, K. Watanabe, T. Taniguchi, S. Tongay, M. F. Crommie, and F. Wang, 2016, ArXiv e-prints eprint 1612.05359.
- Kioseoglou, G., A. T. Hanbicki, M. Currie, A. L. Friedman, and B. T. Jonker, 2016, Scientific reports 6, 25041.
- Kira, M., and S. W. Koch, 2005, The European Physical Journal D 36(2), 143, ISSN 1434-6060.
- Klingshirn, C., 2007, Semiconductor Optics (Springer, Berlin Heidelberg New York), 3rd edition.
- Klots, A. R., A. K. M. Newaz, B. Wang, D. Prasai, H. Krzyzanowska, D. Caudel, N. J. Ghimire, J. Yan, B. L. Ivanov, K. A. Velizhanin, A. Burger, D. G. Mandrus, et al., 2014, Scientific Reports 4, 6608.
- Komsa, H.-P., and A. V. Krasheninnikov, 2012, Phys. Rev. B 86, 241201.
- Kormanyos, A., G. Burkard, M. Gmitra, J. Fabian, V. Zolyomi, N. D. Drummond, and V. Fal'ko, 2015, 2D Materials 2, 022001.
- Kormányos, A., V. Zólyomi, N. D. Drummond, and

G. Burkard, 2014, Phys. Rev. X 4, 011034.

- Korn, T., S. Heydrich, M. Hirmer, J. Schmutzler, and
- C. Schüller, 2011, Applied Physics Letters **99**(10), 102109. Kosmider, K., J. W. González, and J. Fernández-Rossier, 2013, Phys. Rev. B 88, 245436.
- Koster, G. F., R. G. Wheeler, J. O. Dimmock, and H. Statz, 1963, Properties of the thirty-two point groups (MIT Press).
- Kumar, N., Q. Cui, F. Ceballos, D. He, Y. Wang, and H. Zhao, 2014a, Phys. Rev. B 89, 125427.
- Kumar, N., J. He, D. He, Y. Wang, and H. Zhao, 2014b, Nanoscale 6, 12690.
- Lagarde, D., L. Bouet, X. Marie, C. R. Zhu, B. L. Liu, T. Amand, P. H. Tan, and B. Urbaszek, 2014, Phys. Rev. Lett. 112, 047401.
- Lampert, M. A., 1958, Phys. Rev. Lett. 1, 450.
- Latini, S., T. Olsen, and K. S. Thygesen, 2015, Physical Review B 92(24), 245123, ISSN 1098-0121.
- Li, T., , and G. Galli, 2007, The Journal of Physical Chemistry C 111(44), 16192.
- Li, Y., A. Chernikov, X. Zhang, A. Rigosi, H. M. Hill, A. M. van der Zande, D. A. Chenet, E.-M. Shih, J. Hone, and T. F. Heinz, 2014a, Phys. Rev. B 90, 205422.
- Li, Y., J. Ludwig, T. Low, A. Chernikov, X. Cui, G. Arefe, Y. D. Kim, A. M. van der Zande, A. Rigosi, H. M. Hill, S. H. Kim, J. Hone, et al., 2014b, Phys. Rev. Lett. 113, 266804.
- Lien, D.-H., J. S. Kang, M. Amani, K. Chen, M. Tosun, H.- P. Wang, T. Roy, M. S. Eggleston, M. C. Wu, M. Dubey, S.-C. Lee, J.-H. He, et al., 2015, Nano Letters 15(2), 1356.
- Lin, Y., X. Ling, L. Yu, S. Huang, A. L. Hsu, Y.-H. Lee, J. Kong, M. S. Dresselhaus, and T. Palacios, 2014, Nano Letters 14(10), 5569, ISSN 1530-6984.
- Liu, G.-B., W.-Y. Shan, Y. Yao, W. Yao, and D. Xiao, 2013, Phys. Rev. B 88, 085433.
- Liu, H. J., L. Jiao, L. Xie, F. Yang, J. L. Chen, W. K. Ho, C. L. Gao, J. F. Jia, X. D. Cui, and M. H. Xie, 2015a, 2D Materials 2(3), 034004.
- Liu, K.-K., W. Zhang, Y.-H. Lee, Y.-C. Lin, M.-T. Chang, C.- Y. Su, C.-S. Chang, H. Li, Y. Shi, H. Zhang, C.-S. Lai, and L.-J. Li, 2012, Nano Letters 12(3), 1538, pMID: 22369470.
- Liu, X., T. Galfsky, Z. Sun, F. Xia, E.-c. Lin, Y.-H. Lee, S. Kéna-Cohen, and V. M. Menon, 2015b, Nature Photonics $9(1)$, 30.
- Lopez-Sanchez, O., D. Lembke, M. Kayci, A. Radenovic, and A. Kis, 2013, Nature Nanotechnology 8, 497.
- Lopez-Sanchez, O., E. A. Llado, V. Koman, A. F. i Morral, A. Radenovic, and A. Kis, 2014, ACS Nano 8(3), 3042, pMID: 24601517.
- Lundt, N., S. Klembt, E. Cherotchenko, S. Betzold, O. Iff, A. V. Nalitov, M. Klaas, C. P. Dietrich, A. V. Kavokin, S. Höfling, et al., 2016, Nature Communications 7, 13328.
- MacNeill, D., C. Heikes, K. F. Mak, Z. Anderson, A. Kormányos, V. Zólyomi, J. Park, and D. C. Ralph, 2015, Phys. Rev. Lett. 114, 037401.
- Mahan, G. D., 1968, Phys. Rev. 170, 825.
- Mai, C., A. Barrette, Y. Yu, Y. G. Semenov, K. W. Kim, L. Cao, and K. Gundogdu, 2014a, Nano Letters 14(1), 202.
- Mai, C., Y. G. Semenov, A. Barrette, Y. Yu, Z. Jin, L. Cao, K. W. Kim, and K. Gundogdu, 2014b, Phys. Rev. B 90, 041414.
- Maialle, M. Z., E. A. de Andrada e Silva, and L. J. Sham, 1993, Phys. Rev. B 47, 15776.
- Mak, K. F., K. He, Changgu, G. H. Lee, J. Hone, T. F. Heinz, and J. Shan, 2013, Nature Materials 12, 207.
- Mak, K. F., K. He, J. Shan, and T. F. Heinz, 2012, Nat. Nanotechnol. 7, 494.
- Mak, K. F., C. Lee, J. Hone, J. Shan, and T. F. Heinz, 2010, Phys. Rev. Lett. 105, 136805.
- Mak, K. F., and J. Shan, 2016, Nature Photonics 10(4), 216.
- Manca, M., M. M. Glazov, C. Robert, F. Cadiz, T. Taniguchi, K. Watanabe, E. Courtade, T. Amand, P. Renucci, X. Marie, G. Wang, and B. Urbaszek, 2017, Nature Comms. 8, 14927.
- McCreary, K. M., M. Currie, A. T. Hanbicki, H.-J. Chuang, and B. T. Jonker, 2017, ACS Nano 11(8), 7988.
- Meier, F., and B. Zakharchenya, 1984, Modern Problems in Condensed Matter Sciences (North-Holland, Amsterdam). 8.
- Miller, R. C., D. A. Kleinman, A. C. Gossard, and O. Munteanu, 1982, Phys. Rev. B 25, 6545.
- Mitioglu, A., P. Plochocka, A. Granados del Aguila, P. Christianen, G. Deligeorgis, S. Anghel, L. Kulyuk, and D. Maude, 2015, Nano letters 15(7), 4387.
- Mitioglu, A. A., K. Galkowski, A. Surrente, L. Klopotowski, D. Dumcenco, A. Kis, D. K. Maude, and P. Plochocka, 2016, Phys. Rev. B 93, 165412.
- Miwa, J. A., S. Ulstrup, S. G. Sørensen, M. Dendzik, A. G. c. v. a. c. Cabo, M. Bianchi, J. V. Lauritsen, and P. Hofmann, 2015, Phys. Rev. Lett. 114, 046802.
- Molas, M., C. Faugeras, A. Slobodeniuk, K. Nogajewski, M. Bartos, D. Basko, and M. Potemski, 2017, 2D Materials 4(2), 021003.
- Molina-Sánchez, A., D. Sangalli, K. Hummer, A. Marini, and L. Wirtz, 2013, Physical Review B 88(4), 045412.
- Molina-Sánchez, A., and L. Wirtz, 2011, Phys. Rev. B 84, 155413.
- Moody, G., C. Kavir Dass, K. Hao, C.-H. Chen, L.-J. Li, A. Singh, K. Tran, G. Clark, X. Xu, G. Berghäuser, E. Malic, A. Knorr, et al., 2015, Nature Communications 6(May), 8315, ISSN 2041-1723.
- Moskalenko, S. A., 1962, Sov. Phys. Solid State 4, 199.
- Mouri, S., Y. Miyauchi, M. Toh, W. Zhao, G. Eda, and K. Matsuda, 2014, Phys. Rev. B 90, 155449.
- Nagler, P., M. V. Ballottin, A. A. Mitioglu, F. Mooshammer, N. Paradiso, C. Strunk, R. Huber, A. Chernikov, P. C. M. Christianen, C. Schüller, and T. Korn, 2017, ArXiv e-prints eprint 1704.02208.
- Najmaei, S., Z. Liu, W. Zhou, X. Zou, G. Shi, S. Lei, B. I. Yakobson, J.-C. Idrobo, P. M. Ajayan, and J. Lou, 2013, Nature materials 12(8), 754.
- Neumann, A., J. Lindlau, L. Colombier, M. Nutz, S. Najmaei, J. Lou, A. D. Mohite, H. Yamaguchi, and A. Hogele, 2017, Nature Nanotechnology , doi:10.1038/nnano.2016.282.
- Novoselov, K. S., A. K. Geim, S. Morozov, D. Jiang, Y. Zhang, S. Dubonos, I. Grigorieva, and A. A. Firsov, 2004, Science 306, 666.
- Novoselov, K. S., D. Jiang, F. Schedin, T. J. Booth, V. V. Khotkevich, S. V. Morozov, and A. K. Geim, 2005, Proc. Natl Acad. Sci. USA 102, 10451.
- Onga, M., Y. Zhang, R. Suzuki, and Y. Iwasa, 2016, Applied Physics Letters 108(7), 073107.
- Palummo, M., M. Bernardi, and J. C. Grossman, 2015, Nano Letters 15(5), 2794, pMID: 25798735.
- Pelekanos, N. T., J. Ding, M. Hagerott, A. V. Nurmikko, H. Luo, N. Samarth, and J. K. Furdyna, 1992, Phys. Rev. B 45, 6037.
- Perkins, F. K., A. L. Friedman, E. Cobas, P. M. Campbell, G. G. Jernigan, and B. T. Jonker, 2013, Nano Letters
- Piermarocchi, C., F. Tassone, V. Savona, A. Quattropani, and P. Schwendimann, 1997, Phys. Rev. B 55, 1333.
- Plechinger, G., P. Nagler, A. Arora, R. Schmidt, A. Chernikov, A. G. del Aguila, P. C. Christianen, R. Brats- ´ chitsch, C. Schüller, and T. Korn, 2016, Nature Communications 7, 12715.
- Plechinger, G., P. Nagler, J. Kraus, N. Paradiso, C. Strunk, C. Schller, and T. Korn, 2015, physica status solidi (RRL) " Rapid Research Letters $9(8)$, 457, ISSN 1862-6270.
- Poellmann, C., P. Steinleitner, U. Leierseder, P. Nagler, G. Plechinger, M. Porer, R. Bratschitsch, C. Schüller. T. Korn, and R. Huber, 2015, Nature Materials 14(9), 889, ISSN 1476-1122.
- Pospischil, A., M. M. Furchi, and T. Mueller, 2014, Nature nanotechnology $9(4)$, 257.
- Press, D., T. D. Ladd, B. Zhang, and Y. Yamamoto, 2008, Nature 456(7219), 218.
- Qiu, D. Y., T. Cao, and S. G. Louie, 2015, Phys. Rev. Lett. 115, 176801.
- Qiu, D. Y., F. H. da Jornada, and S. G. Louie, 2013, Phys. Rev. Lett. 111, 216805.
- Radisavljevic, B., A. Radenovic, J. Brivio, V. Giacometti, and A. Kis, 2011a, Nature. Nanotech. 6, 147.
- Radisavljevic, B., M. B. Whitwick, and A. Kis, 2011b, ACS Nano 5(12), 9934, pMID: 22073905.
- Raja, A., A. Chaves, J. Yu, G. Arefe, H. M. Hill, A. F. Rigosi, T. C. Berkelbach, P. Nagler, C. Schüller, T. Korn, et al., 2017, Nature Communications 8, 15251.
- Ramasubramaniam, A., 2012, Phys. Rev. B 86, 115409.
- Ribeiro-Soares, J., R. M. Almeida, E. B. Barros, P. T. Araujo, M. S. Dresselhaus, L. G. Cancado, and A. Jorio, 2014, Phys. Rev. B 90, 115438.
- Rigosi, A. F., H. M. Hill, K. T. Rim, G. W. Flynn, and T. F. Heinz, 2016, Physical Review B 94(7), 075440, ISSN 2469- 9950.
- Rivera, P., J. R. Schaibley, A. M. Jones, J. S. Ross, S. Wu, G. Aivazian, P. Klement, N. J. Ghimire, J. Yan, D. G. Mandrus, W. Yao, and X. Xu, 2015, Nature Communications 6, 6242.
- Rivera, P., K. L. Seyler, H. Yu, J. R. Schaibley, J. Yan, D. G. Mandrus, W. Yao, and X. Xu, 2016, Science 351(6274), 688.
- Robert, C., D. Lagarde, F. Cadiz, G. Wang, B. Lassagne, T. Amand, A. Balocchi, P. Renucci, S. Tongay, B. Urbaszek, and X. Marie, 2016, Phys. Rev. B 93, 205423.
- Rösner, M., C. Steinke, M. Lorke, C. Gies, F. Jahnke, and T. O. Wehling, 2016, Nano Letters 16(4), 2322.
- Ross, J. S., P. Klement, A. M. Jones, N. J. Ghimire, J. Yan, D. G. Mandrus, T. Taniguchi, K. Watanabe, K. Kitamura, W. Yao, D. H. Cobden, and X. Xu, 2014, Nature Nanotechnology 9, 268.
- Ross, J. S., S. Wu, H. Yu, N. J. Ghimire, A. M. Jones, G. Aivazian, J. Yan, D. G. Mandrus, D. Xiao, W. Yao, et al., 2013, Nature communications 4, 1474.
- Rybkovskiy, D. V., I. C. Gerber, and M. V. Durnev, 2017, Phys. Rev. B 95, 155406.
- Rycerz, A., J. Tworzydlo, and C. J. Beenakker, 2007, Nature. Phys. 3, 172.
- Rytova, N. S., 1967, Proc. MSU, Phys., Astron. 3, 30.
- Salehzadeh, O., M. Djavid, N. H. Tran, I. Shih, and Z. Mi, 2015, Nano Letters 15(8), 5302.
- Sallen, G., L. Bouet, X. Marie, G. Wang, C. R. Zhu, W. P. Han, Y. Lu, P. H. Tan, T. Amand, B. L. Liu, and B. Ur-

baszek, 2012, Phys. Rev. B 86, 081301.

- Schaibley, J. R., H. Yu, G. Clark, P. Rivera, J. S. Ross, K. L. Seyler, W. Yao, and X. Xu, 2016, Nature Reviews Materials 1, 16055.
- Schmidt, R., A. Arora, G. Plechinger, P. Nagler, A. Granados del Aguila, M. V. Ballottin, P. C. M. Christianen, ´ S. Michaelis de Vasconcellos, C. Schüller, T. Korn, and R. Bratschitsch, 2016a, Phys. Rev. Lett. 117, 077402.
- Schmidt, R., G. Berghäuser, R. Schneider, M. Selig, P. Tonndorf, E. Malić, A. Knorr, S. Michaelis de Vasconcellos, and R. Bratschitsch, 2016b, Nano Letters 16(5), 2945.
- Selig, M., G. Berghäuser, A. Raja, P. Nagler, C. Schüller, T. F. Heinz, T. Korn, A. Chernikov, E. Malic, and A. Knorr, 2016, Nature Communications 7(May), 13279, ISSN 2041-1723.
- Shang, J., X. Shen, C. Cong, N. Peimyoo, B. Cao, M. Eginligil, and T. Yu, 2015, ACS Nano 9(1), 647, pMID: 25560634.
- Shi, H., H. Pan, Y.-W. Zhang, and B. I. Yakobson, 2013a, Phys. Rev. B 87, 155304.
- Shi, H., R. Yan, S. Bertolazzi, J. Brivio, B. Gao, A. Kis, D. Jena, H. G. Xing, and L. Huang, 2013b, ACS Nano 7(2), 1072.
- Shinada, M., and S. Sugano, 1966, Journal of the Physical Society of Japan 21(10), 1936.
- Sidler, M., P. Back, O. Cotlet, A. Srivastava, T. Fink, M. Kroner, E. Demler, and A. Imamoglu, 2016, Nature Physics .
- Sie, E. J., A. J. Frenzel, Y.-H. Lee, J. Kong, and N. Gedik, 2015a, Phys. Rev. B 92, 125417.
- Sie, E. J., J. W. McIver, Y.-H. Lee, L. Fu, J. Kong, and N. Gedik, 2015b, Nature materials 14(3), 290.
- Singh, A., G. Moody, K. Tran, M. E. Scott, V. Overbeck, G. Berghäuser, J. Schaibley, E. J. Seifert, D. Pleskot, N. M. Gabor, J. Yan, D. G. Mandrus, et al., 2016a, Phys. Rev. B 93, 041401.
- Singh, A., G. Moody, S. Wu, Y. Wu, N. J. Ghimire, J. Yan, D. G. Mandrus, X. Xu, and X. Li, 2014, Phys. Rev. Lett. 112, 216804.
- Singh, A., K. Tran, M. Kolarczik, J. Seifert, Y. Wang, K. Hao, D. Pleskot, N. M. Gabor, S. Helmrich, N. Owschimikow, U. Woggon, and X. Li, 2016b, Phys. Rev. Lett. 117, 257402.
- Slobodeniuk, A., and D. Basko, 2016a, 2D Materials 3(3), 035009.
- Slobodeniuk, A. O., and D. M. Basko, 2016b, Phys. Rev. B 94, 205423.
- Smith, R. J., P. J. King, M. Lotya, C. Wirtz, U. Khan, S. De, A. O'Neill, G. S. Duesberg, J. C. Grunlan, G. Moriarty, J. Chen, J. Wang, et al., 2011, Advanced Materials 23(34), 3944.
- Song, X., S. Xie, K. Kang, J. Park, and V. Sih, 2016, Nano Letters 16(8), 5010.
- Splendiani, A., L. Sun, Y. Zhang, T. Li, J. Kim, C.-Y. Chim, G. Galli, and F. Wang, 2010, Nano Letters 10, 1271.
- Srivastava, A., and A. Imamoglu, 2015, Phys. Rev. Lett. 115, 166802.
- Srivastava, A., M. Sidler, A. V. Allain, D. S. Lembke, A. Kis, and A. Imamoğlu, 2015, Nature Physics.
- Stébé, B., and A. Ainane, 1989, Superlattices and Microstructures 5(4), 545.
- Steinhoff, A., J.-H. Kim, F. Jahnke, M. Rösner, D.-S. Kim, C. Lee, G. H. Han, M. S. Jeong, T. O. Wehling, and C. Gies, 2015, Nano Letters 15(10), 6841.
- Steinhoff, A., M. Rösner, F. Jahnke, T. O. Wehling, and

C. Gies, 2014, Nano letters 14(7), 3743, ISSN 1530-6992.

- Steinleitner, P., P. Merkl, P. Nagler, J. Mornhinweg, C. Schller, T. Korn, A. Chernikov, and R. Huber, 2017, Nano Letters 17(3), 1455.
- Stier, A. V., K. M. McCreary, B. T. Jonker, J. Kono, and S. A. Crooker, 2016a, Nature Communications 7(10643), 10643.
- Stier, A. V., N. P. Wilson, G. Clark, X. Xu, and S. A. Crooker, 2016b, Nano Letters 16(11), 7054.
- Stroucken, T., and S. W. Koch, 2015, Journal of Physics: Condensed Matter 27(34), 345003.
- Sun, D., Y. Rao, G. A. Reider, G. Chen, Y. You, L. Br@zin, A. R. Harutyunyan, and T. F. Heinz, 2014, Nano Letters 14(10), 5625, pMID: 25171389.
- Suris, R. A., 2003, Optical Properties of 2D Systems with Interacting Electrons (Springer Netherlands).
- Szczytko, J., L. Kappei, J. Berney, F. Morier-Genoud, M. T. Portella-Oberli, and B. Deveaud, 2004, Phys. Rev. Lett. 93, 137401.
- Taniguchi, T., and K. Watanabe, 2007, Journal of Crystal Growth $303(2)$, 525.
- Tonndorf, P., R. Schmidt, P. Böttger, X. Zhang, J. Börner, A. Liebig, M. Albrecht, C. Kloc, O. Gordan, D. R. Zahn, et al., 2013, Optics express 21(4), 4908.
- Tran, K., A. Singh, J. Seifert, Y. Wang, K. Hao, J.-K. Huang, L.-J. Li, T. Taniguchi, K. Watanabe, and X. Li, 2017, Phys. Rev. B 96, 041302.
- Trolle, M. L., G. Seifert, and T. G. Pedersen, 2014, Phys. Rev. B 89, 235410.
- Trushin, M., M. O. Goerbig, and W. Belzig, 2016, Phys. Rev. B 94, 041301.
- Ugeda, M. M., A. J. Bradley, S.-F. Shi, F. H. da Jornada, Y. Zhang, D. Y. Qiu, S.-K. Mo, Z. Hussain, Z.-X. Shen, F. Wang, S. G. Louie, and M. F. Crommie, 2014, Nature Materials 13, 1091.
- Ulstrup, S., A. G. Čabo, J. A. Miwa, J. M. Riley, S. S. Grønborg, J. C. Johannsen, C. Cacho, O. Alexander, R. T. Chapman, E. Springate, M. Bianchi, M. Dendzik, et al., 2016, ACS Nano 10(6), 6315, ISSN 1936-0851.
- Vasilevskiy, M. I., D. G. Santiago-Pérez, C. Trallero-Giner, N. M. R. Peres, and A. Kavokin, 2015, Phys. Rev. B 92, 245435.
- Vinattieri, A., J. Shah, T. C. Damen, D. S. Kim, L. N. Pfeiffer, M. Z. Maialle, and L. J. Sham, 1994, Phys. Rev. B 50, 10868.
- Volmer, F., S. Pissinger, M. Ersfeld, S. Kuhlen, C. Stampfer, and B. Beschoten, 2017, Physical Review B 95(23), 235408.
- Wang, F., G. Dukovic, L. Brus, and T. Heinz, 2005, Science 308, 838.
- Wang, G., L. Bouet, M. M. Glazov, T. Amand, E. L. Ivchenko, E. Palleau, X. Marie, and B. Urbaszek, 2015, 2D Materials 2(3), 034002.
- Wang, G., L. Bouet, D. Lagarde, M. Vidal, A. Balocchi, T. Amand, X. Marie, and B. Urbaszek, 2014, Phys. Rev. B 90, 075413.
- Wang, G., I. C. Gerber, L. Bouet, D. Lagarde, A. Balocchi, M. Vidal, E. Palleau, T. Amand, X. Marie, and B. Urbaszek, 2015, 2D Materials 2, 045005.
- Wang, G., X. Marie, I. Gerber, T. Amand, D. Lagarde, L. Bouet, M. Vidal, A. Balocchi, and B. Urbaszek, 2015a, Phys. Rev. Lett. 114, 097403.
- Wang, G., X. Marie, B. L. Liu, T. Amand, C. Robert, F. Cadiz, P. Renucci, and B. Urbaszek, 2016a, Phys. Rev. Lett. 117, 187401.
- Wang, G., E. Palleau, T. Amand, S. Tongay, X. Marie, and B. Urbaszek, 2015b, Applied Physics Letters 106(11), 112101.
- Wang, G., C. Robert, M. M. Glazov, F. Cadiz, E. Courtade, T. Amand, D. Lagarde, T. Taniguchi, K. Watanabe, B. Urbaszek, and X. Marie, 2017, ArXiv e-prints eprint 1704.05341.
- Wang, G., C. Robert, A. Suslu, B. Chen, S. Yang, S. Alamdari, I. C. Gerber, T. Amand, X. Marie, S. Tongay, and B. Urbaszek, 2015, Nature Comms. (6), 10110.
- Wang, H., K. Ferrio, D. G. Steel, Y. Z. Hu, R. Binder, and S. W. Koch, 1993, Physical Review Letters 71(8), 1261.
- Wang, H., L. Yu, Y.-H. Lee, Y. Shi, A. Hsu, M. L. Chin, L.-J. Li, M. Dubey, J. Kong, and T. Palacios, 2012a, Nano Letters 12(9), 4674.
- Wang, H., C. Zhang, W. Chan, C. Manolatou, S. Tiwari, and F. Rana, 2016b, Phys. Rev. B 93, 045407.
- Wang, Q., S. Ge, X. Li, J. Qiu, Y. Ji, J. Feng, and D. Sun, 2013, ACS Nano 7(12), 11087.
- Wang, Q. H., K. Kalantar-Zadeh, A. Kis, J. N. Coleman, and M. S. Strano, 2012b, Nature nanotechnology 7(11), 699.
- Wang, Z., L. Zhao, K. F. Mak, and J. Shan, 2017, Nano Letters 17(2), 740.
- Wilson, J., and A. Yoffe, 1969, Advances in Physics 18(73), 193.
- Withers, F., O. D. Pozo-Zamudio, S. Schwarz, S. Dufferwiel, P. M. Walker, T. Godde, A. P. Rooney, A. Gholinia, C. R. Woods, P. Blake, S. J. Haigh, K. Watanabe, et al., 2015, Nano Letters 15(12), 8223.
- Wu, F., F. Qu, and A. H. MacDonald, 2015a, Phys. Rev. B 91, 075310.
- Wu, S., S. Buckley, J. R. Schaibley, L. Feng, J. Yan, D. G. Mandrus, F. Hatami, W. Yao, J. Vučković, A. Majumdar, and X. Xu, 2015b, Nature 520(7545), 69.
- Xenogiannopoulou, E., P. Tsipas, K. Aretouli, D. Tsoutsou, S. Giamini, C. Bazioti, G. Dimitrakopulos, P. Komninou, S. Brems, C. Huyghebaert, et al., 2015, Nanoscale 7(17), 7896.
- Xia, F., H. Wang, D. Xiao, M. Dubey, and A. Ramasubramaniam, 2014, Nature Photonics 8(12), 899.
- Xiao, D., G.-B. Liu, W. Feng, X. Xu, and W. Yao, 2012, Phys. Rev. Lett. 108, 196802.
- Xiao, D., W. Yao, and Q. Niu, 2007, Phys. Rev. Lett. 99, 236809.
- Xu, X., D. Xiao, T. F. Heinz, and W. Yao, 2014, Nature Physics 10, 343.
- Yan, T., J. Ye, X. Qiao, P. Tan, and X. Zhang, 2017, Phys. Chem. Chem. Phys. 19, 3176.
- Yang, L., W. Chen, K. M. McCreary, B. T. Jonker, J. Lou, and S. A. Crooker, 2015a, Nano letters 15(12), 8250.
- Yang, L., N. A. Sinitsyn, W. Chen, J. Yuan, J. Zhang, J. Lou, and S. A. Crooker, 2015b, Nature Physics .
- Yang, W., J. Shang, J. Wang, X. Shen, B. Cao, N. Peimyoo, C. Zou, Y. Chen, Y. Wang, C. Cong, et al., 2016, Nano letters 16(3), 1560.
- Yao, W., D. Xiao, and Q. Niu, 2008, Phys. Rev. B 77, 235406.
- Ye, Y., Z. J. Wong, X. Lu, X. Ni, H. Zhu, X. Chen, Y. Wang, and X. Zhang, 2015, Nature Photonics 9(11), 733, ISSN 1749-4885.
- Ye, Z., T. Cao, K. O'Brien, H. Zhu, X. Yin, Y. Wang, S. G. Louie, and X. Zhang, 2014, Nature 513, 214.
- Ye, Z., D. Sun, and T. F. Heinz, 2017, Nature Physics 13, 26.
- You, Y., X.-X. Zhang, T. C. Berkelbach, M. S. Hybertsen, D. R. Reichman, and T. F. Heinz, 2015, Nature Physics
- Yu, H., X. Cui, X. Xu, and W. Yao, 2015a, National Science Review $2(1)$, 57.
- Yu, H., X. Cui, X. Xu, and W. Yao, 2015b, National Science Review $2(1)$, 57.
- Yu, H., G.-B. Liu, P. Gong, X. Xu, and W. Yao, 2014, Nature communications 5.
- Yu, H., Y. Wang, Q. Tong, X. Xu, and W. Yao, 2015c, Physical review letters 115(18), 187002.
- Yu, T., and M. W. Wu, 2014, Phys. Rev. B 89, 205303.
- Yu, T., and M. W. Wu, 2016, Phys. Rev. B 93, 045414.
- Yu, Y., Y. Yu, C. Xu, A. Barrette, K. Gundogdu, and L. Cao, 2016, Phys. Rev. B 93, 201111.
- Yun, W. S., S. W. Han, S. C. Hong, I. G. Kim, and J. D. Lee, 2012, Phys. Rev. B 85, 033305.
- van der Zande, A. M., P. Y. Huang, D. A. Chenet, T. C. Berkelbach, Y. You, G.-H. Lee, T. F. Heinz, D. R. Reichman, D. A. Muller, and J. C. Hone, 2013, Nature materials $12(6)$, 554.
- Zeng, H., J. Dai, W. Yao, D. Xiao, and X. Cui, 2012, Nat. Nanotechnol. 7, 490.
- Zhan, Y., Z. Liu, S. Najmaei, P. M. Ajayan, and J. Lou, 2012, Small 8(7), 966.
- Zhang, C., Y. Chen, A. Johnson, M.-Y. Li, L.-J. Li, P. C. Mende, R. M. Feenstra, and C.-K. Shih, 2015a, Nano Letters 15(10), 6494, pMID: 26389585.
- Zhang, C., A. Johnson, C.-L. Hsu, L.-J. Li, and C.-K. Shih, 2014a, Nano Letters 14(5), 2443, pMID: 24783945.
- Zhang, X., X.-F. Qiao, W. Shi, J.-B. Wu, D.-S. Jiang, and P.-H. Tan, 2015b, Chem. Soc. Rev. 44, 2757.
- Zhang, X., X.-F. Qiao, W. Shi, J.-B. Wu, D.-S. Jiang, and P.-H. Tan, 2015c, Chem. Soc. Rev. .
- Zhang, X.-X., T. Cao, Z. Lu, Y.-C. Lin, F. Zhang, Y. Wang, Z. Li, J. C. Hone, J. A. Robinson, D. Smirnov, et al., 2017, Nature Nanotechnology doi:10.1038/nnano.2017.105, .
- Zhang, X.-X., Y. You, S. Y. F. Zhao, and T. F. Heinz, 2015d,

Phys. Rev. Lett. 115, 257403.

- Zhang, Y., T.-R. Chang, B. Zhou, Y.-T. Cui, H. Yan, Z. Liu, F. Schmitt, J. Lee, R. Moore, Y. Chen, H. Lin, H.-T. Jeng, et al., 2014b, Nature Nanotechnology 9, 111.
- Zhang, Y., T. Oka, R. Suzuki, J. Ye, and Y. Iwasa, 2014c, Science 344(6185), 725.
- Zhao, C., T. Norden, P. Zhao, Y. Cheng, P. Zhang, F. Sun, P. Taheri, J. Wang, Y. Yang, T. Scrace, K. Kang, S. Yang, et al., 2016, Nature Nanotechnology doi:10.1038/nnano.2017.68, .
- Zhao, W., Z. Ghorannevis, L. Chu, M. Toh, C. Kloc, P.-H. Tan, and G. Eda, 2013a, ACS Nano 7(1), 791.
- Zhao, W., R. M. Ribeiro, M. Toh, A. Carvalho, C. Kloc, A. H. Castro Neto, and G. Eda, 2013b, Nano Letters 13(11), 5627.
- Zhong, D., K. L. Seyler, X. Linpeng, R. Cheng, N. Sivadas, B. Huang, E. Schmidgall, T. Taniguchi, K. Watanabe, M. A. McGuire, et al., 2017, Science Advances 3(5), e1603113.
- Zhou, J., W.-Y. Shan, W. Yao, and D. Xiao, 2015, Phys. Rev. Lett. 115, 166803.
- Zhou, Y., G. Scuri, D. S. Wild, A. A. High, A. Dibos, L. A. Jauregui, C. Shu, K. de Greve, K. Pistunova, A. Joe, T. Taniguchi, K. Watanabe, et al., 2017, Nature Nanotechnology doi:10.1038/nnano.2017.106, .
- Zhu, B., X. Chen, and X. Cui, 2015, Scientific Reports 5, 9218.
- Zhu, B., H. Zeng, J. Dai, Z. Gong, and X. Cui, 2014a, Proceedings of the National Academy of Sciences 111(32), 11606.
- Zhu, C. R., K. Zhang, M. Glazov, B. Urbaszek, T. Amand, Z. W. Ji, B. L. Liu, and X. Marie, 2014b, Phys. Rev. B 90, 161302.
- Zhu, Z. Y., Y. C. Cheng, and U. Schwingenschlögl, 2011, Phys. Rev. B 84, 153402.